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# A High-Level Computer Graphics Implementation of <br> Three-Dimensional B-Spline Surface Generation 

 by
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A thesis submitted in partial fulfillment of the requirements for the degree of

Master of Science

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1987

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A HIGH-LEUEL COMPUTER GRAPHICS IMPLEMENTATION OF THREE-DIMENSIDNAL B-SPLINE SURFACE GENERAIION
by Dennis Michael Bryant
Chairperson of the Supervisory Committee:
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The difficulty of accurately defining, representing and visualizing three-dimensional sculptured surfaces has concerned designers and engineers throughout history, but never more so than today. Technology has given man the ability, and the necessity, to build autamobile bodies, ship hulls and aircraft fuselages with complex curvature and extremely smooth lines. The ability to efficiently develop and define the form of such surfaces has not kept pace with the requirement to manufacture them.

Ihis study explores the application of a surface Bspline for surface definition coupled with high-level computer graphics to enhance visualization. A computer program, SPLINE, is introduced which Eacilitates interactive construction of the B-spline control graph and real-time manipulation of the model on an Evans and Sutherland PS 300 distributed graphics system. A uniform nonrational surface B-spline is utilized for interactive modeling, with the capability preprogrammed of implementing nonunifarm rational surface B-splines upon

later addition of an inversion algorithm.
While the program is not fully Eunctional, due to apparent shortcomings of the host computer operating system, the viability and desirability of such a system is fully demonstrated. Heuristic techniques are discussed for approaching model development, based on properties of the B-spline and characteristics of SPLINE. Step-by-step illustrated case studies further develop the modeling techniques. Examples include the generation of B-spline representations of a sailing yacht hull and of a Porsche automobile body, as well as the freeform development of a sculptured surface ab initio.

Structured and heavily commented pragram listings are included, with Flow diagrams, Function netwarks, and operating instructions. Program expansions and hardware improvements are recommended and existing provisions within the program for these improvements are identified.

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DEDICATION

To Linda,
For her patience.
horteptaza

BYnat at


## CHAPIER 1

## SCULPIURED SURFACE REPRESENTATION

### 1.1. Sculptured Surfaces

The computer program described herein was developed to demonstrate the feasibility of designing and defining sculptured surfaces through the use of a B-spline algorithm coupled with highly interactive computer graphics. The accurate definition, representation, and visualization of three-dimensional surfaces is a problem which has concerned designers and engineers throughout histary. Even relatively simple three-dimensional shapes can often be difficult to depict on a two-dimensional drawing such that the viewer can readily generate a mental image of the object or the craftsman can construct the abject true to the designer's intentions.

Particularly troublesome, however, are sculptured surfaces, those having curvature in more than one direction. Sculptured surfaces form a vital part of aircraft, ship, and automobile designs, being necessary in aircraft and ship design for aerodynamic and hydrodynamic streamlining and used extensively in automobile design primarily for styling reasons. Nor is the use of these troublesome surfaces for the sake of appealing to the eye restricted to such major market items as automobiles; as Rogers and Satterfield [1] point out, today even the
shampoa bottle is likely to spart a complex sculptured surface.

Given the difficulty of representing these surfaces in a two-dimensional medium, it is not surprising that the historical solution has often been simply to avoid producing such drawings at all. Letcher [2] presents a brief but interesting history of man's attempts to skirt the problem in the context of ship hull design. The form of the earliest hulls, and of many small craft in lowtechnology cultures today, was undoubtedly preserved by carving a salid model from wood. Later, the use of the master-section-and-batten method was developed and has continued to some extent until today. A few transverse sections are erected with the desired form, and the remainder of the hull is defined bu the installation of the hull planking as it is sprung about the master sections.

Even as late as the early 1900's, the lines drawing was not the principal tool in developing and visualizing the lines of a ship's hull. While the lines were ultimately preserved with such a drawing, they were usually taken from a carved model. Often the model was even carved in a material with separable layers so that the lines could be directly traced onto the paper.
1.2. The Ship's Lines Drawing

The problem of defining and representing a sculptured
surface is perhaps best illustrated by a description of the lines drawing, that instrument which is used to develop and define the surface of ship and boat hulls. As is standard with the representation of virtually all three-dimensional objects, three views of the hull are presented on the lines drawing: a top view (known as the half-breadth plan, because only one half of the symmetrical hull is shown); a front view (known as the body plan, and which actually is a stern view as welly, and a side or profile view (labeled the sheer plan).

Intersections of the vessel's hull with evenly spaced cutting planes are projected onto these three reference planes. On the body plan, the form of the hull at transverse sections is shown. Depending on the size and complexity of the vessel's hull, the sections are shown at ten, twenty or forty foot intervals, with a few intermediate stations shown in areas of greatest curvature. For the sheer plan, vertical cutting planes are taken at one to four foot intervals, yielding a set of buttocks lines. Waterlines are similarly generated on the half-breadth plan by intersecting the hull with vertical longitudinal cutting planes. Nonorthogonal cutting planes further serve to define the shape through the production of diagonals or cant lines. A sample lines drawing is shown in figure 1.

The task of the naval architect in developing a



completed set of lines is not an easy one. Having visualized the desired form, the architect must accurately translate it into a set of lines on paper which satisfies quantitative, qualitative, and aesthetic considerations. Working with irregularly shaped curves, the designer must nevertheless maintain specific areas within the curves to yield proper ship stability and handling characteristics. In order to obtain fair (smooth) lines, the lines are drawn with a drafting spline, an elastic lath constrained by weights called ducks. The lines must not only be smooth and contain the appropriate areas, but the projection of all points on the lines onto all three reference planes must be consistent. These requirements often appear to be nearly mutually exclusive.

In short, because of the difficulties of (1) visualizing the sculptured surface, (2) obtaining smooth lines, (3) maintaining agreement of all views, and (4) achieving and measuring the required form characteristics such as section areas, the design of a ship's lines is a tedious and difficult iterative task for even the most experienced architect. Letcher [2] cites Kinney as saying, "'It takes between five and ten working days for an experienced man to produce a good set of lines,' regardless of the size of the vessel." He also points out that anything more than a slight change requires starting over almost from the beginning.

When the naval architect has finished the lines drawing, however, the task of hull definition is not yet complete. The lines are next translated into a tabulated Form called a table of offsets. Ihis table lists the distances, at each station, of waterlines from the centerline and of buttocks lines above the baseline. An example is shown in table 1.

Greater accuracy is needed for production purposes than is obtainable from the relatively small scale lines drawings. For this reason the lines are redrawn full size on a large wooden floor (the mold loft) and faired again. In very recent practice, the full scale lofting may be replaced by drawing the lines in one-sixteenth scale on a marble slab with a very hard pencil or by entering the offsets into a computer for generation of a large scale drawing on a plotter. In any case, the large scale Fairing is used to identify necessary revisions to the lines and to produce a more accurate table of offsets. 1.3. Mathematicallu Defined Surfaces

It is not hard to understand, then, the benefits which would be derived if the hull form, or shampoo bottle, could be defined by a precise mathematical relationship. The need for full scale lofting would be eliminated, since accuracy could be obtained initially to whatever degree was desired. Precision would no longer depend upon the ability to measure small increments on a

## TABLE 1

Table of Dffsets for a Mariner Class Vessel
Source: Dwen [3]
(Dimensions given in feet, inches and eighths)

| Station |  | WL | , | WL |  | WL | WL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (FWD END) | 1 |  |  |  |  |  |  |
| 0 FP | i | --- | ; | 3-0-5 |  | 2-8-5 | 1-0-1 |
| 1/2 | I | -- | ; | 4-8-7 | I | 5-0-7 | 4-3-5 |
| 1 | ; | -- | ; | 6-10-2 | ' | 7-11-6 | 8-6-1 |
| 2 | ' | 2-4-0 | ' | 13-7-6 | ; | 16-9-3 | 19-9-0 |
| 3 | ; | 9-2-0 | ; | 24-1-0 | ' | 27-7-1 | 30-10-3 |
| 4 | ' | 21-4-0 | 1 | 33-3-0 | ' | 35-8-1 | 37-2-2 |
| 5 | ' | 28-5-6 | 1 | 36-2-6 | + | 37-10-3 | 38-0-0 |
| 6 |  | 24-10-4 | ! | 34-8-1 | , | 37-0-7 | 37-11-7 |
| 7 | ; | 13-6-4 | ; | 27-1-4 | \| | 31-2-6 | 35-8-1 |
| 8 |  | 4-5-2 | ; | 15-0-3 | ; | 19-3-3 | 26-2-2 |
| 9 | I | --- | ; | 6-0-7 |  | 7-9-4 | 11-2-4 |
| $91 / 2$ | ' | --- | ; | 2-8-7 | ' | 3-4-1 | 4-3-0 |
| AP 10 | i | --- | ; | --- | ; | -- | -- |

Heights Above Molded Baseline

Station
(FWD End)
0 FP
$1 / 2$
1
2
3
4
5
6
7
6
9
9
9
AP 10
(Aft End)
$4-f t$ : $\quad$-ft i 16-ft i 24-ft buttock : buttock : buttock : buttock
47-5-6 | 57-0-7
2-3-0 ; 40-8-3 ; 55-4-4
0-11-7
$0-0-4$
$0-8-7$
$0-0-0$


14
6-9-5 ;
$\begin{array}{l:l}0-6-7 \\ 0-0-0 & \end{array}$
---

- 0-0-0
---
4-9-6
21-11-3
30-3-6
2-1-0
$0-0-0$
$1-2-1$
14-3-4
23-4-1
28-5-0
31-6-5
38-11-3
$13-3-3$
$30-0-4$

37-1-4
41-7-0
44-1-6
38-4-5

drawing, but could be achieved by simply outputting a few more digits from the computer's memory.

Preparation of a table of offsets would not be a manual task, but simply a matter of solving the mathematical relationship at any desired point on the surface. Thus the representation would not only be more accurate, but could be more complete as well. A lines drawing only accurately defines the surface at points which fall exactly on the lines drawn. Determination of intermediate points requires drawing and fairing additional lines or performing some manner of interpolation. Interpolation will yield only a rough approximation, given the complex curvature of the form. A mathematical representation can be equally accurate at any point which is defined by the mathematical relationship.

A mathematical representation could also provide direct input for the calculation of stability data, as well as for fabrication. The need for scale model testing would be greatly reduced with the substitution of computer simulations, which would no longer need to rely upon mere approximations of the form.

Perhaps most exciting are the prospects for using a mathematical representation of a sculptured surface as input to a numerically controlled machining (NCM) process. Rogers, Rodriguez, and Satterfield have already reported substantial progress in this application [4,5,6]. A
system of computer programs was developed on a microprocessor-based graphics system interfaced with a CNC controller to drive a milling machine for the production of wooden towing tank models. The numerical control milling data base is actually generated directly by a computer program from a mathematical definition of the hull. This mathematical definition is created by the program in response to manipulation of a graphical image on the computer screen by the user. Using this system, towing tank models have been produced in only two days.

Considering the beleaguered state of the shipbuilding and automotive industries in the United States today, it is impossible not to become excited with the possibilities of larger scale implementations of this concept. 1.4. High-Level Computer Graphics

The implementation of mathematical definition of sculptured surfaces does not require enormous computing power. The FAIRLINE series of computer programs developed by Letcher $[2,7,8]$ for the design of sailing yacht hulls was designed for use on a Texas Instruments pocket calculator. On the other hand, defining the surface is only part of the problem. Closely related is the problem of representing the surface during the surface development process and subsequent to surface definition. It may be difficult to visualize a three-dimensional surface while looking at a two-dimensional drawing, but it is even more

difficult to visualize a complex sculptured surface by reviewing a computer-generated table of coordinates.

It is when coupled with high-level computer graphics that the mathematical representation begins to be as useful as it is powerful. Kigh-level computer graphics have been defined by Calkins [9] as being characterized by:

> (1) the ability to display three-dimensional objects,
(2) real-time image manipulation of the threedimensional objects displayed, and
(3) color-shaded object surfaces.

Calkins summarizes high-level computer graphics as the "capability of real time manipulation of realistically rendered 3-dimensional objects." (It will be shown later that while the computer system utilized for the research described in this paper does not meet the third criterion, it certainly fulfills the intention of this summation. With high-level computer graphics, the designer can rotate the object about to obtain another perspective or zoom in on a troublesome detail. The results of changes made in one view can be immediately reviewed fram other angles to determine their suitability.

It is this merging of visualization of sculptured surfaces through high-level computer graphics and definition by mathematical representation which has been

explored in this research.

## CHAPTER 2

B-SPLINE SURFACES

The form of mathematical surface representation selected for implementation in the computer program under consideration is the surface B-spline. In particular, a nonuniform rational surface B-spline algorithm has been utilized, though in its present form the pragram only allows the user direct contral of a subset of this, the uniform rational surface B-spline.

The B-spline concept was developed by Schoenberg [10] in 1946 and introduced to computer-aided geametric design by Riesenfeld [11] in 1973. Several properties of the Bspline curve or surface generation algorithms make them very suitable for sculptured surface modeling using interactive computer graphics. Briefly, the B-spline offers inherent curve smoothing, considerable data compression (complex surfaces can be fully defined with a small amount of data), local contral (a portion of a curve or surface can be modified without affecting the entire surface, the flexibility of including sharp discontinuities in a curve or surface, and a convenient means of interactively manipulating the curve.

This last property will be shown to be a particularly useful characteristic. Barsky and Greenberg [12] discuss the difficulty of performing shape design using

mathematical methods which require the designer to directly specify values for algarithm variables. It can require an intimate knowledge of complex mathematics for a designer to be able to readily perceive the necessary adjustment to a mathematical algorithm which will effect the desired change in a portion of a surface. In contrast, modeling with B-splines requires virtually no knowledge of mathematics by the program user. Fish [13] observed, "The nice thing about spline curves is that they allow you to treat a collection of pieces of various polynomials as a single entity, maintaining continuity of tangent directions, curvatures, and so on without working at it." Undoubtedly the same considerations led Rogers [4], warking with a number of mathematical curve representations, to conclude that the B-spline was "most generally useful."

While a detailed understanding of the mathematics behind B-splines is not necessary in order to use them, some understanding will nevertheless aid the user in developing the ability to mare quickly model a desired surface. A brief introduction follows. Mare extensive treatments of the subject can be found in Rogers and Adams [14], who provide useful examples, and in Bartels, Beatty, and Barsky [15], who provide a particularly methodical and understandable approach.


### 2.1. Parametric Curves

The Cartesian coordinate system is essential to most surface design. It is in this coordinate system that most of the formulations are presented with which the naval architect or aircraft engineer will wark to determine the performance characteristics of the craft. It is also Cartesian coordinates in which the graphics computer will require data to be presented for display and manipulation on the screen. At the same time, the Cartesian coordinate system has significant liabilities when warking with sculptured surfaces.

Most significantly, many sculptured surfaces or curves cannot be defined by an explicit function (a function having only ane value of $y$ for each value of $x$. . The transverse section of a ship with tumble-home is a ready example. Also, it will be shown that calculating one Cartesian coordinate for a curve at even increments of another Cartesian coordinate can result in very irregular definition resalution. For these reasons, a parametric representation is preferable. The B-spline can be parametric. In a parametric representation, the Cartesian coordinate for a point on a curve is not defined in terms of the other Cartesian coordinate (i.e. $y=f(x)$ ), but coordinates are instead defined as functions of a parametric variable: thus,

$$
x=f(u)
$$

anden
and

$$
y=g(u)
$$

where $\psi$ is the parametric variable.
The parametric representation addresses both of the objections to the purely Cartesian coordinates. Implicit functions in $x$ and $y$ can be handled without ambiguity and the resolution of the curve representation is generally much more uniform with equal parameter spacing than with equal Cartesian coordinate spacing.

Rogers and Adams [14] provide an illustration similar to figure 2, which compares representations of a circular arc using a nonparametric representation with data points at equal $x$ intervals, using uniform parametric spacing, and using equal arc lengths. The nonparametric representation uses the relationship,

$$
\begin{equation*}
y=\sqrt{ }\left(1-x^{2}\right) \tag{1}
\end{equation*}
$$

The uniform parametric spacing uses a parameter, $u$, which varies from zero to one. The points on the curve are defined by

$$
x=\left(1-u^{2}\right) /\left(1+u^{2}\right)
$$

and

$$
\begin{equation*}
y=2 u /\left(1+u^{2}\right) \tag{2}
\end{equation*}
$$

The equal arc length representation defines the points on the curve as

$$
x=\cos \theta
$$

and


$$
\begin{equation*}
y=\sin \theta . \tag{3}
\end{equation*}
$$

In each case, the arc is represented by a straight-line connection between six points.


Fig. 2. Comparison of parametric and nonparametric representations.

While the uniform parametric spacing does not produce a resolution quite as uniform as that of equal arc lengths, it is clearly superior to the equal $x$ coardinate spacing. Sharpe and Thorne [15] discuss an approach for using the equal arc length spacing with a parametric representation, but more straightforward equal parameter spacing was felt to be sufficient for the purposes of this program.

### 2.2. Two-Dimensional B-Splines

The B-spline is most easily understood initially by looking at a two-dimensional uniform nonrational case, the simplest form of the B-spline. The B-spline curve is a piecewise palynomial curve. That is, the curve is braken into segments which are defined by separate polynomials.


This curve is everywhere continuous, both in position and in up to the $(K-2)$ derivative, $K$ being the order of the spline.

The general $B$-spline curve is defined by:

$$
\begin{align*}
& D(U)=\sum_{I=1}^{n} B_{I} N_{I, k}(U)  \tag{4}\\
& N_{I, I}(U)=1 \text { if } x_{I \leq U<X_{I+1}} \\
& =0 \text { otherwise } \\
& N_{I, K(U)}=\frac{\left(U-x_{I}\right) N_{I, k-1}(U)}{x_{I+k-1}-x_{I}}+\frac{\left(x_{I+K-U)} N_{I+1, k-1}(U)\right.}{x_{I+K-X_{I+1}}}
\end{align*}
$$

where

$$
\begin{aligned}
D(u)= & {[x(u), y(u)], \text { the curve, } } \\
n \quad= & \text { number of control vertices, } \\
B_{I}= & \text { control vertices' coordinates, } \\
K= & \text { order of the B-spline curve (implies } \\
& \text { degree }(K-1)), \\
N_{I, K}(U)= & B-s p l i n e \text { basis functions, }
\end{aligned}
$$

and
$x_{x}-$ elements of the knot vector.
While it can be seen that the B-spline algorithm can be somewhat confusing mathematically, the use of it is actually quite intuitive. The curve being formed is shaped by controlling a relatively small number of points known as control points or vertices. The curve will not interpolate (pass through) the control vertices, but will mimic the overall shape of the array of vertices. For a

better visualization of this, the vertices are frequently jained by straight line segments, forming a control polygon. An example cantral palygan with its assaciated B-spline curve is shown in figure 3. The vertices are represented by the squares, the contral polygon by the connecting straight line segments, and the B-spline curve by the curved line.

polygon

An apt analogy to the effect of the control vertices upon the curve is that of a set of magnets to a ferrous wire. While the curve does not pass directly through the contral vertices, it is molded by their placement, being drawn toward them as if toward magnets. Moving a control
vertex pulls the curve in the vertex's local region in the direction of the movement. Placing vertices close together creates a stronger effect on the curve in the region of those vertices.

Every point on the curve is a weighted average of the position of a number of control vertices. Each vertex has a unique basis function, which defines the weight of the vertex with respect to the parameter $u$. These basis functions, polynomials in the parametric variable, are independent of the shape of the controlling polygon, being completely defined by the order ( $k$ ) and a knot vector.

The knot vector divides the curve parameter (u) into a series of discrete values. This subdivides the B-spline curve into a series of segments defined by separate polynomials. The joined segments form a piecewise polynomial curve. If the divisions in the curve are equal (the knot vector specifies uniform step width between knots), the B-spline is said to be uniform.

The parameter $\&$ varies between an initial value and some final maximum as the curve is traversed. Values of $«$ that correspond to joints between the spans are called knots. In the case of a uniform B-spline, the knots will typically correspond to integer values of $u$. The knot vector gives the sequence of these knots and is constrained to be non-decreasing. Thus the knot vector defines the range of the parameter $\&$ which corresponds to

each segment of the curve.
When the knot vector is specified, a multiplicity $k$ at each end of the knot vector ensures that the ends of the curve interpolate the first and last vertices in the control polygon. This is a very convenient constraint when performing modeling with a B-spline. The knot vector For a uniform third order B-spline with four vertices, which varies from zero to $(n-K+1)$, is $[0,0,0,1,2,2,2]$.

The basis functions, then, indicate the degree and extent of the influence of each control vertex. This provides the lacal contral which was mentioned above. The maximum extent of influence of a single control vertex in


Fig. 4. Localized effect of moving a single contral vertex.

parameter space is plus or minus half the order of the basis function. Conversely, the shape of every span is affected by $K$ successive vertices. Figure 4 illustrates the localized effect of moving a single control vertex.

A comparison of figures 5 and 6 will demonstrate the effect of curve order upon the basis functions. Figure 5 shows the values for the basis functions for a third order curve with five vertices. Figure 6 shows the basis function values for a fourth order curve, also with five vertices. In each case, the parameter $\&$ has been normalized to unity. Notice that the basis functions for the fourth order curve are generally lower in value at any given value of $«$, but are nonzero over a greater range. Thus a higher order basis function yields a curve which is less markedly influenced locally by the movement of a single control vertex, but which is smoother and more taut than a lower order curve. This effect can be readily visualized by examining figures 7 and 8 , which show third and fourth order $B-s p l i n e$ curves created by the same control polygons.

A few characteristics of the B-spline curve will be convenient to keep in mind when manipulating a curve:
(1) The B-spline curve will have at most as many extreme and inflection points as the control polygon.
(2) A straight line will be produced in the $B$ -


Fig. 5. Third order basis functions for five vertices.


Fig. 6. Fourth order basis functions for five vertices.


Fig. 7. Third order B-spline curve.


Fig. B. Fourth order B-spline curve.
spline curve by $K$ collinear contral vertices.
(3) K-1 collinear contral vertices will yield a curve tangent to the contral polygon.
(4) A knuckle, or sharp discontinuity, will accur at the point where $K-1$ control vertices are colocated. An example is shown in figure 9.


Fig. 9. Knuckle produced by calocated vertices.
(5) Each span of a B-spline curve of order $k$ lies within the convex hull of its $k$ associated vertices. An illustration of this concept is shown in figure 10 , where the $B$-spline curve wauld lie in the shaded

## area.

As previously mentioned, an advantage of the B-spline is the resultant data compression. Rogers and Satterfield [1] present an example wherein they successfully represented the forebody of a U.S. Navy ammunition ship using only a five by eight polygonal net with twodimensional uniform B-splines.

### 2.3. Surface B-Splines

Nearly all systems developed for computer-aided sculptured surface design have defined the surface in terms of a net of lines. Typically, a series of B-spline curves in parallel planes is intersected with another series of curves in planes perpendicular to the first. The result is not a true surface definition, but definition of a net of lines lying on the surface. Io define any point not lying on a net line requires an interpolative approximation.

The program which is the subject of this study uses a true surface algorithm rather than such a network of twodimensional representations. The surface created is a mosaic of surface patches, just as the two-dimensional curve was a piecewise polynomial curve, and the surface, like the curve, is everywhere continuous with continuity of the derivatives to a degree dependent upon the order of the basis functions. Control is achieved through manipulation of a net of control vertices, with the


Fig. 10. The convex hull of a third order (a), fourth order (b) and fifth order (c) polygon.
control graph being analogous to the control polygon of the two-dimensional case. The control graph, as well as the surface, is three-dimensional.

The surface (or tensor-product) B-spline is defined very similarly to the two-dimensional spline as:

$$
\begin{aligned}
& N_{X_{1}}(U)=1 \text { if } x_{x} \leq U<X_{x+1} \\
& \text { = O otherwise } \\
& M_{J_{1}}(u)=1 \text { if } y_{0 \leq u<y o+1} \\
& \text { - O otherwise } \\
& N_{X_{1} K}(U)=\frac{\left(U-x_{I}\right) N_{I, k-1}(U)}{x_{I+K-1}-x_{I}}+\frac{\left(x_{I+K}-U\right) N_{I+1, k-1}(U)}{x_{I+K-x_{I+1}}}
\end{aligned}
$$

where

| $Q(u, w)=$ | $[x(u, w), y(u, w), z(u, w)], \quad$ surface data |
| ---: | :--- |
|  | points, |
| $u, w=$ | parametric variables, |
| $n=$ | number of control vertices in the $u$ |
|  | direction, |
| $m=$ | number of control vertices in the $w$ |
|  | direction, |
| $B_{x .0}=$ | control graph points, |
| $K=$ | order of the surface in the $u$ |
|  | direction, |



| $L=$ | order of the surface in the $w$ |
| ---: | :--- |
|  | direction, |
| $N_{I, k}(U)=$ | basisffunctions in the $u$ direction, |
| $M_{J . L}(w)=$ | basisffunctions in the $w$ direction, |
| $X_{I}=$ | elements of the knot vector in the $u$ |
|  | direction, |

and
yo - elements of the knot vector in the $w$ direction.

The computer program developed for this study implements a very direct approach to surface calculation, computing all basis functions initially, then performing the summation of equation (5). A more efficient algorithm, based on the work of Cox and de Boor, is presented in appendix $[-27$ of Rogers and Adams [14].

The surface B-spline is directly analogous to the two-dimensional B-spline in virtually every way, having very similar properties extended into three dimensions. For example, just as the effect of moving a single control vertex was seen in two dimensions in figure 4 , the effect in three dimensions is shown in figure 11. (The effect extends toward the back of the picture the same as toward the front, although some of that effect is lost to view in this illustration due to depth cueing.

One difference between the two and three-dimensional B-splines is the effect of a repeated knot vector. A


Fig. 11. Localized effect of moving a single control vertex in a surface B-spline.
knuckle can be introduced into a two-dimensional curve by use of a repeating knot value in the knot vector. The same is not true with a three-dimensional surface, unless the knuckle is desired across the entire surface, since the same knot vector is used for all sets of vertices in the $u(a r w)$ direction. Repeating a knot for one or two positions in the contral graph will result in repeated knot values for the corresponding positions in all sets of vertices in the net. For this reason, knuckles will be introduced into the surface in this program only by colocating vertices. Multiple vertices will not indicate repeated knot values. Ihis concept is dealt with in more
depth by Rogers and Satterfield [1,17].

### 2.4. Nonuniform Rational B-Splines

The B-spline algorithm implemented in this program is a still more general case of the surface $B$-spline, the nonuniform rational B-spline (NURB). Both non-uniformity and rationality extend the power of the algorithm, as explained by Tiller [18].

A limitation of nonrational B-splines is the inability to accurately represent circles, conics, and quadric primitives. The rational B-spline can do so. Rationality refers to the addition of a fourth coordinate. Given a point in three-dimensional Euclidean space, $P=(x, y, z)$, a corresponding point is now defined in fourdimensional space, $\mathrm{PH}^{H}=(\mathrm{HX}, \mathrm{Hy}, \mathrm{Hz}, \mathrm{H})$. The $H$ is the homogeneous coordinate and is constrained to be non-zero. By adding a homogeneous coordinate to the definition of each control vertex, the effect of that vertex is effectively scaled. Thus the B-spline algorithm now becomes:

$$
\begin{equation*}
Q^{H}(U, w)=\sum_{I=1}^{n} \sum_{J=1}^{m} B^{H} I_{\ldots J} N_{I \ldots k}(U) M_{J} L(w) . \tag{6}
\end{equation*}
$$

Application of the rational B-spline to the development of surfaces is further dealt with by Tiller.

As alluded to above, the knot vector spacing can also be used in some cases to control the surface shape. Thus the algorithm implemented in this program will allow
电
nonuniform knot vectors.
Because of their tremendous power and flexibility, nonuniform rational B-splines have been recognized now as an IGES standard for curve and surface definition [19]. The Alpha_1 project at the University of Utah Computer Science Department, working with Riesenfeld, has done much work in exploring the potential of NURB's [13].

Dn the other hand, manipulation of the homogeneous coordinates and of the knot vector does not produce intuitively predicted results. Since this negates one of the greatest advantages of the B-spline for interactive modeling, the user of the computer program developed in this work has not been given direct control over these variables. Uniform knot spacing, and a homogeneous coordinate of one, are default values for interactive modeling. By including these variables in the algorithm, though not under user control, the potential of utilizing nonuniform rational B-splines in an inversion algorithm (discussed in chapter 6) is retained.


## CHAPTER 3

SPLINE: A B-SPLINE SURFACE MODELING PROGRAM

The end product of this study is a computer program for the Evans and Sutherland PS 300 computer graphics warkstation which Eacilitates the design and representation of sculptured surfaces using a surface Bspline. This program is known as SPLINE.
3.1. Hardware

The PS 300 is a distributed graphics system, employing its awn micropracessar for the processing of display-related data and relying upon a host computer for other operations. The host used in the development of this pragram 15 the PDP-11/44 with an RSX-11M+ operating system. The computer is the University of Washington's Mechanical Engineering Department camputer and is set up an a time sharing system. Memory far execution of individual programs is limited to 64 kilobytes, with extension to 128 kilabytes possible by specifying an ID flag during compilation. This Elag overrides the reservation of memory normally restricted to system housekeeping tasks.

The PS 300 station which was used is the single-user version of the Evans and Sutherland graphıcs workstation. Properly designated the PS 330, this unit is the most basic system of the PS 300 family and 15 commonly referred
to by the family designation. The unlt upon which this program was developed was running Ps Version ${ }^{\text {g firmware, } a}$ preliminary version of the operating system and proprletary programming language. The PS 300 workstation is pictured in figure 12. As can be seen there, the workstation $1 s$ comprised of the control unit, display screen, keyboard, data tablet, and control dials.


Fig. 12. PS 300 workstation.
The contral unit consists of a Graphics Contral Processor, mass memory, and the Display Processor. The Graphics Control Processor is a Motorola 68000 mlcroprocessor with $24-b i t$ address space and 256 kilobytes of local memory for the graphics firmware. A full megabyte 15 available 10 mass memory, with 16-bit
communication with the Graphics Contral Processor and 32bit communication with the Display Processor, for very fast display access.

The PS 300 display screen is a monochrome vector refresh display with 8192 by 8192 resalution. White lines and characters are displayed on a black screen with sixtyfour levels of intensity. While solids with color shading cannot be displayed, the fine scaling of intensity allows display of wire frame models which are unusually easy to interpret. Ihrough a feature called depth cueing, the intensity of lines is gradually decreased as their distance behind the plane of the screen is increased. Ihis fading with depth helps to give the perception of three dimensions while viewing a model on the twodimensional screen.

An additional benefit of depth cuelng is that wire frame lines in the background can be clipped from view, eliminating confusion with foreground lines. Ihis is especially important since the PS 300 does not provide hidden line removal. A comparison of figures 13 and 14 will illustrate this advantage.

The keyboard doubles as an input device for the PS 300 and a terminal for the host computer. Features include a full keyboard and twelve programable function keys with LED labels. A separate pad with eight programable control dials also features LED labels.


Fig. 13. Wire Erame madel wlthaut depth cueing.


Fig. 14. Wire frame model with depth cueing.

The coordinate position of a stylus on the data tablet is converted to a digital equivalent for the positioning of a cursor on the screen. This can be programmed for menu selection or picking of paints or lines on a displayed model.

The PS 300 performs graphical manipulations and the associated mathematical transformations independently from the host. Ihe transformations and matrix concatenations are accomplished without the user having to program the matrix arithmetic.

While graphics manipulations can be performed without host interaction, communication between the host computer and the PS 300 is essential for virtually all applications. The PS 300 has no local storage capability, so its program must be stored on the host system and passed to the PS 300 's memory as ASCII data. The programming language available on the PS 300, which is unique to Evans and Sutherland systems, is highly efficient for graphics display and manipulation, but other mathematics and data processing which would be straightforward in another high level computer language can be very difficult. The programmer must make a division of the graphics application into graphics processing and analysis functions in accordance with each computer's strengths. An intelligent division can minimize communication between the computers, but
substantial communication will remain necessary.
Communication between the PS 300 and the host is accomplished through a 9600 baud interface. Data transfer protocol is established thraugh the PS 300 Host-Resident I/O Subroutines (PSID's). These are host-resident FORTRAN subroutines which provide two-way communication between the computers.

### 3.2. Programming the PS 300

The PS 300 has its own high level ASCII command language with English-like commands, detailed in the Evans and Sutherland manual, PS 300 Computer Graphics Sustem [20]. Structured objects are created and accessed by name with commands such as UECTOR_LIST cto create an object as a list of vectors), TRANSLATE, ROTATE, and SCALE (to perform the named operations?.

Models are created as hierarchical groupings of graphical data, transformations applied to the data, and attributes such as intensity and level of detail. Primitive objects are defined and used to bulld more complex objects. For example, an automobile wheel might be defined by means of a vector list, then instances of that wheel translated and rotated to create four wheels and position them relative to a separately defined body, forming a representation of a car. A sample display tree is shown in figure 15. The three basic forms of display tree nodes can be seen there: data nodes (such as vector


Fig. 15. Display tree for an automobile.
lists defining objects), operation nodes (such as translations and rotations), and instance nodes. Instance nodes group other elements together under a single name. Applying a transformation to an element results in the transformation of all subordinate elements as well.

Manipulation and contral of models is accomplished through the creation of function networks. Values from interactive devices such as function keys or control dials are processed through user-designed function networks and applied to interaction polnts in the model's structure. The function networks are combinations of connected black box functions. These function blocks accept data, manipulate it according to predefined rules for the given function, and output new values to another function input or to interaction points in the display tree.

For example, ADDER might be defined as an instance of the function, F:ADDC, which sums any number sent to its first input and a constant value held on its second input. If the function keys are connected to input one of $A D D E R$ and the integer " 2 " is sent to the second input, whenever a function key is pressed ADDER will output an integer equal to two plus the number of the key. The programming statements to accomplish this would be:

> ADDER: $=F:$ ADDC; \{Defines ADDER as an instance of the function, ADDC. $\}$

SEND FIX(2) TO <2>ADDER; \{Puts the value, 2, on

ADDER's constant input. $\}$ CONNECI FKEYS<1>:<1>RDDER; \{Connects Eunction key
output to ADDER's
trigger input. 3

CONNECT ADDER<1>:[input and name of the element to which the sum is to be sent]
\{Routes output to desired location.3.

Available functions include mathematical operations, Boolean logic operations, routing functions, and data conversion.

### 3.3. SPLINE

Figure 16 presents an overview of SPLINE, showing the interrelationship of major hardware and software components. Items marked by dashed lines have not yet been implemented, but provision for future addition of these features has been made within the program architecture and source coding. All programming on the PDP-11 was performed in FQRTRAN language and all programming on the PS 300 was in the language described above. A more detailed description of the programs is contained in appendix $A$ and the Full FORTRAN and PS 300 program listings are contained in appendices $B$ and $C$, respectively.


Fig. 15. Querview of SPLINE.
whether it is desired to perform a freeform ab initio design or to represent a previously known surface with a B-spline. In respect to this distinction, wu, Abel and Greenberg [21] distinguish between shape design and shape representation. Ihey identify shape design as having a primary concern of conceiving, displaying and modifying complex forms. Shape representation, on the other hand, is characterized by a need to describe or approximate existing surfaces for the purpose of graphical manipulation to enhance visualization or for geometric calculation to permit quantification. SPLINE will allow both approaches, shape design (freeform surface design) and shape representation (modeling a B-spline surface to approximate a previously known surface).

If it is desired to represent a known surface, data points on that surface may be input through a two or three-dimensional digitizer or by direct creation of an appropriately formatted data file. The program will allow screen display of these known points for direct visual comparison with the B-spline surface during modeling. In either case, the user must select the number and initial relative position of the control vertices (by designating the size and shape of a planar matrix of points), as well as the order of the surface in respect to each of the parametric directions. Provision has been made for future addition of an inversion algorithm, which would calculate
initial control vertex locations to appraximate known surface data.

The contral vertices, the B-spline surface and known surface points may be displayed on the screen in any combination through Eunction key menu selections, and can be rotated, translated, or scaled in real time through use of the control dials. The B-spline surface is Formed and modified by moving the contral vertices about the screen. Vertex movement is communicated to the FORTRAN program, which recalculates the $B-s p l i n e ~ s u r f a c e ~ a n d ~ s e n d s ~ a ~ n e w ~$ vector list to the PS 300.

Vertices are selected for movement by using the stylus on the data tablet to locate a cross hair on the screen over the desired vertex for picking. Individual vertices or entire rows or columns of vertices may be selected for movement. Movement is defined by manipulation of labeled control dials.

Ihrough the use of z-clipping, narrow sections of the model may be viewed without display of the remainder of the structures. This enables very accurate comparisons of any combination of display elements to be made very easily.

B-spline surfaces are displayed as nets of constant parameter lines. Provision has been made For future implementation of orthogonal plane intersection mapping, which would enable display of more traditional
representations, such as waterlines and transverse section lines, yet based on the B-spline surface.

### 3.4. Operating Sustem Limitations

At this time the functionality of the program is severely limited by what appears to be a problem in the operating system or FDRIRAN compiler of the PDP-11 camputer.

During programming, it was noted that previously trouble-free subroutines would often fail after adding seemingly unrelated lines of FQRIRAN program. Ihis was found to be caused by variables changing value during program execution, but not under program control. Efforts to eliminate or program around this problem were not successful. Discussion with the Mechanical Engineering Department computer system manager and with Professor Ganter of the thesis committee revealed that the PDP-11 suffers from known operating system and compiler flaws which cause addressing problems resulting in similar symptams.

While the exact manifestation of the problem varied with the state of program development, the current symptoms include failure of the host-resident input/output library subroutines (PSID's) after execution of the subroutine which calculates the B-spline surface. This precludes display of the B-spline surface. A slightly earlier version of the program will allow the B-spline
surface to be calculated and displayed, but at an indeterminate time afterward will refuse to answer further calls to the communication subroutines. This usually prevents modification of the B-spline surface once displayed.

Troubleshooting efforts have included careful review of the program for any definition of array elements outside of dimensioned array size, successful operation of each subroutine independently, and attempts to reestablish communication immediately after failure. The problem was further clouded by consultation with the Evans and Sutherland Software Technical Support Department [22], which indicated that use of the PSIO subroutines has been discontinued in favor of more reliable communication packages and that there are documented and undocumented flaws in the preliminary PS 300 operating systems such as the one used for development of SPLINE. Nevertheless, as will be shown in chapter 5, the project results are sufficiently successful to demonstrate the viability of such a computer program.


## CHAPIER 4

## OPERATING INSIRUCIIONS

4.1. Preparing Known Surface Data

If it is desired to display known points from a Surface for purposes of modeling a B-spline representation of the known surface, this data must be properly formatted before entering SPIINE. The data will automatically be correctly formatted by the digitizing program if it is prepared through use of the two-dimensional digitizing program, DIGIT, or the three-dimensional digitizing program, DIGIT3. However, the first parameter in the global header may need to be adjusted (see below).

The PREPS input format is used for the preparation of known surface data. PREPS is a data pre-processor used at the University of washington for conversion of data describing the geometry of an object into a PS 300 syntaxcompatible data file. The input file format for PREPS has been adopted as the standard for data input to SPLINE in order to facilitate the use of SPLINE with other PREPScompatible programs, such as DIGIT and DIGITヨ.

The PREPS input file format is detailed in Calkins' laboratory book [23]. A summary follows.

The data file format prescribes a global header followed by a series of subheaders, each with an assoclated set of substructure data. SPLINE will allow

the display of individual data points represented in the data file, as well as lines sequentially connecting the data points within a substructure. Division of a structure into substructures will provide the most meaningful display if the substructures correspond to logical divisions in the actual structure. A common choice is the representation of profile lines or section contours as individual substructures.
4.1.1 The global header. The global header is the first group of data in the PREPS-format data file and contains information affecting the display of all substructures. SPLINE reads the data with a list-directed Format, so the exact format of the data in the file is not important. However, the correct sequence must be maintained.

The global header contains five parameters:

1. 2NORM the normalization factor for all data point coordinate values. This parameter should be set to the largest absolute value of any $x, y$, or $z$ coordinate.
2. INSTRI not used by SPLINE. Should be set to 1.
3. XBODY global translation of all data in the input file along the $x$ axis. SPLINE assumes that the
normalized data runs from 0 to 1. If the origin is not actually at ane end of the structure, use this to mave the structure accordingly for the most convenient display.
4. YBODY the same as XBODY, for the $y$ coordinate.
5. ZBODY the same as XBODY, for the $z$ coordinate.
4.1.2. Substructure headers. Each set of substructure data is comprised of seven subheader parameters immediately followed by the substructure data. The subheader parameters are:
6. NPTS the number of data points in the substructure.
7. NPTS2 the number of repetitions of this substructure to be displayed. Normally set to 1 . If several identical substructures are to be displayed, this can be set to the number or repetitions and ICOORD to the coordinate which varıes between repetitions. The series of varied coordinate values is then entered for that coordinate
in the data, one per substructure repetition. Examples appear in [23].
8. ICOORD the coordinate which remains constant within a substructure, or varies between repeated substructures.

$$
\begin{aligned}
\text { ICOORD } & =1, x \text { coordinate } \\
& =2, y \text { coordinate } \\
& =3, z \text { coordinate } \\
& =0, \text { no repetition. }
\end{aligned}
$$

4. XIRAN translation of the substructure, in non-normalized coordinates, along the $\times$ axis.
5. YIRAN the same as XIRAN, for the $y$ axis.
6. 2IRAN
the same as XIRAN, for the $z$ axis.
7. IREF1
the plane about which mirror image reflection occurs.

$$
\begin{aligned}
\text { IREF1 } & =1, y z \text { plane } \\
& =2, x z \text { plane } \\
& =3, x y \text { plane } \\
& =0, \text { no reflection } .
\end{aligned}
$$

For modeling purposes, it is usually best to select no
reflection, as discussed in chapter 5.
4.1.3. Substructure data. Each subheader is immediately followed by the correspanding substructure data. The data is not paired for each point, but is listed with all $x$ coordinates first, all y coordinates next, and all $z$ coordinates last. If ICOORD is not set to O, only ane value is entered for the constant coordinate, except as noted under NPTS2, above.

A sample data file is presented below, including a global header and subheader with substructure data. Comments contained in brackets are not part of the data file.
3.

## [2NORM]

1000 [INSTRT, $00 x, y, z$ translation.] $61 \quad 1 \quad$ [First subheader; 6 points, one substructure, $\times$ coordinate constant for substructure.J

0000 [No translation, no reflection.]
$0.585 \mathrm{E}+00$
$-0.255 \mathrm{E}+00-0.202 \mathrm{E}+00-0.191 \mathrm{E}+00$
-0.157E+00 -0.861E-01 -0.0 [6 y values.]
$-0.962 E+00-0.711 E+00 \quad-0.586 E+00$
-0.4日2E+00 -0.370E+00 -0.362E+00 [6 z values.]

| 7 | 1 | 1 | [Begin second substructure header.] |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |

$0.255 \mathrm{E}+01$ [Begin second substructure data ....]

### 4.2. Preparing the Computer Sustem

In order to run SPLINE, both the PS 300 computer and the host PDP-11 must be operational. Before logging on to the host, it is suggested that the PS 300 be readied.

SPLINE requires PS Version 8 firmware on the PS 300. The version can be checked by removing and inspecting the disk installed in the lower right-hand corner of the PS 300 cabinet. If it is necessary to reload the firmware, use the following sequence:

1. Turn on the power switch located on the display screen.
2. Turn off the power switch located on the upper right-hand corner of the PS 300 cabinet.
3. Insert the PS Uersion 8 disk.
4. Turn on the cabinet power switch.
5. Wait for the DUAL LINE READY message on the display screen, which should appear in about five minutes.

It will be necessary to log on to the PDP-11 in the normal manner in order to run SPLINE.

### 4.3. SPLINE Operating Instructions

After logging on to the PDP-11 computer, execute the program by entering "RUN SPLINE." A series of

"Working..." statements will begin to appear on the screen as the $P S$ 300's program file is read from the disk and passed from the host computer to the PS 300 under FORTRAN program control.
4.3.1. Initial Eormatting selections. After loading the PS 300 program, the LED indicators on the PS 300 keyboard and control dials will contain illuminated labels and a series of questions will be presented on the PDP-11 terminal screen.

The initial question is, "Do you wish to display a known surface from a PREPS-format file?" Answer "Y" or " $N$ ", for yes or no. If a "Y" is entered, the user will be prompted for the name of the data file containing the PREPS-formatted data. See "Preparing Known Surface Data" above.

The next series of questions asks the user to specify the size of the initial contral vertex matrix (i.e. 8,5) and the length-to-width ratio of the matrix. The maximum matrix dimensions which can be selected are ( 10,8 ). The minimum dimensions are (5,5). The initial control vertices will be positioned in the $x y$ plane at $z=0$, with the user's first response representing the number of contral vertices $1 \pi$ the $x$ direction and the second response controlling the number of vertices $1 \pi$ the $y$ direction. The selected length-to-width ratio will determine the relative spacing between control vertices in

$-2$
$=-1$
E

| 6. | - | = | - |
| :---: | :---: | :---: | :---: |

2. Mactury
$-2$
the $x$ direction (length) and that in the $y$ direction (width). Figure 17 illustrates the initial contral vertex matrix resulting from selecting a matrix size of ( $B, 5$ ) with a length-to-width ratio of 3.

The user is finally prompted to select the arder of the B-spline in the longitudinal ( $u$ ) and transverse (w) directions. Ihird or fourth order B-splines may be selected. AFter entering the selections, small cubes representing the control vertices will begin to appear on the PS 300 screen.


Fig. 17. An $8 \times 5$ matrix of control vertices with a length/width ratio of 3 .
4.3.2. Enabling the PS 300 keyboard. AEter all initial formatting selections have been made (in response
to display screen prampts), the fallowing message will appear on the screen:

PRESS <SHIFT-IINE/LOCAL>
ON THE PS-300 KEYBOARD
FOLLOWED BY <IERM>

The LINE/LOCAL and TERM keys are located in the keypad at the left side of the PS 300 keyboard. Press the LINE/LOCAL key while holding down the SHIFT key. This enables the twelve function keys at the top of the keyboard. Press the TERM key if it is desired to remove the text display from the screen.
4.3.3. Control dials. The control dials are labeled by LED indicators and have the following functions:

Global $X$ moves the model in the $x$ direction in the screen coordinate system (left and right).

Global $Y$ moves the model in the $y$ diraction in the screen coordinate system (up and down).

GLOBAL 2 moves the model in the $z$ direction in the screen coordinate system (in and out of the screen). As the model moves into the screen (away from the viewer) past the $z=0$ plane, depth cueing will cause portions of the model to fade, creating the illusion
of depth. Depth cueing can be disabled by moving the entire model forward of the $z=0$ plane (toward the viewer) with the GLOBAL 2 dial.

SCALING scales the entire display, allowing the user to examine details of the display more closely.

ROTATE $X$ rotates the model about the screen's $x$ (horizontal) axis.

ROIATE $Y$ rotates the model about the screen's $y$ (vertical) axis.

ROIATE 2 rotates the model about the screen's z axis ©turning it within the plane of the screen).
4.3.4. Main menu. The LED labels above the keyboard function keys present the main menu, from which SPLINE functions are selected. The following options are available:

F1 UERIICES is a three-way toggle controlling the display of the control vertices. Vertices are displayed on the screen as small cubes. Pressing the Fi key selects one of the following options, in sequence:
(1) vertices displayed,
(2) vertices displayed with straight
lines connecting them in matrix position order,
(3) vertices not displayed.

F2 B-SPLINE toggles display of the B-spline surface on and off. When the F2 key is pressed, the B-SPLINE label above the key will blink while the host computer calculates a vector list for the B-spline surface and sends it to the PS 300 . When the surface is displayed, the label will cease blinking.

F3 KNOWN PT is a three-way toggle controlling the display of known surface points contained in a PREPS-format file. Points are displayed as asterisks (*'s). Pressing the F3 key selects one of the following options, in sequence:
(1) known points are displayed,
(2) known points are displayed and points within substructures are connected in sequence by straight lines,
(3) known points are not displayed.
interactive modeling mode, glving the user the ability to manipulate control point positions. When the Fly key is pressed, several Eunction key and control dial labels change to indicate new assigned functions or availability of previously assigned functions. Interactive modeling is discussed in section 4.3.5 below.

F5 CLIP toggles z-clipping on and off. when z-clipping is enabled, only portions of the model lying within a narrow band parallel to the plane of the screen can be viewed. Ihis allows slices or sections of the model to be viewed without confusion caused by lines in front of and behind the section being examined. When the FS key is pressed, the screen will be blanked and a CIIPPING label will appear above the eighth control dial. Turning the dial slightly will cause a slice of the model to be displayed. Adjusting the CLIPPING dial wll vary the depth of the slice which is displayed. By turning the GLOBAL $z$
dial, it is passible to move the model through the clipping window, allowing the viewing of any portion of the model. Note that it is possible to move the model entirely outside of the clipping window, in which case it cannot be viewed.

FG REFLECI has not been implemented. When implemented, it will toggle on and off the display of a reflection of the model about its $X Z$ plane. This label will not be displayed during interactive modeling, indicating that the reflection function is not available at that time. 〔Inis prevents the updating of the reflected surface from slowing down the computer's response to interactive inputs during modeling.J

F7 XY has not been implemented. When implemented, this key will toggle on and off the display of intersections of the $X Y$ plane cbody-fixed coordinates) with the B-spline surface. On a ship model, this corresponds to the display of

|  |  | waterlines. Ihis function is not |
| :---: | :---: | :---: |
|  |  | available during interactive modeling. |
| FB | $x 2$ | has not been implemented. When |
|  |  | implemented, it will Function |
|  |  | similarly to the F7 key, described |
|  |  | above, and will display lines |
|  |  | corresponding to a ship's buttocks |
|  |  | lines. |
| F9 | $Y Z$ | has not been implemented. When |
|  |  | implemented, it will Eunction |
|  |  | similarly to the F7 key, described |
|  |  | above, and will display lines |
|  |  | corresponding to transverse sections |
|  |  | of a ship hull. |
| F10 | I/0 | selects the input/output menu. |
|  |  | Pressing this key causes the labels |
|  |  | above the function keys to display a |
|  |  | menu of input and output functions |
|  |  | described in section 4.3.6, below. |
| F11 | RESEI | is a three-way toggle which resets the |
|  |  | displayed model to each one of three |
|  |  | orthogonal views, in sequence. |
|  |  | Pressing the Fll key resets the scale |
|  |  | factor and global translations to |
|  |  | those of the initial display and |
|  |  | orients the $X Y, X Z$, or $Y Z$ plane of the |


model parallel to the screen. Repeatedly pressing the key will cycle the display through the three orientations. This Eunction key is particularly useful when orienting the model for display of slices with the CLIP Eunction.

F12 QUII stops execution of the program and initializes the PS 300, clearlng the screen. If it is desired to use the keyboard to communicate with the host computer at this point, press the IERM key to return the screen to a text display mode, then press the LINE/LOCAL key, fallowed by RETURN. The host computer's prompt should now be visible.
4.3.5. Interactive modeling. The interactive modeling mode is entered and exited by pressing the INTERACT (F4) key. This mode is the heart of the computer program, allowing the user to select and relocate control vertices in order to mold a B-spline surface.

When the F4 key is pressed, the labels above the three global translation control dials cGlobal X, Global Y, and GLOBAL 2) change to UERTEX X, UERTEX Y, and UERTEX $Z$ and begin to blink. These dials can now be used
to move the selected vertex in the indicated direction in the body-fixed coordinate systew. If it is necessary to move the entire body, the glabal translation functions can be restored by toggling the interactive modeling function off with the F4 key. The blinking labels will remind the user, while in the interactive modeling mode, that dial movement will relocate vertices rather than translate the entire model, in order to prevent inadvertent movement of vertices.

Individual contral vertices are selected for movement with the stylus and data tablet. When the tip of the stylus is placed near the surface of the data tablet, a tracking cross will appear on the screen. By moving the stylus lightly over the data tablet surface, the tracking crass can be pasitianed aver the desired contral vertex. The vertex is then selected by pressing the stylus momentarily against the data tablet surface while keeping the cursar positianed aver the contral vertex. Ihis activates a switch in the tip of the stylus, causing the data tablet to report the stylus position, leading to identification of the selected vertex. The vertex can then be moved into the desired position with the vertex translation dials. If it is necessary to rearient the model in order to obtain a better view or reduce ambiguity for the selection or location of contral vertices, this may be accomplished with the rotation dials or RESEI

function key, which remain operational while in the interactive modeling mode.

When a control vertex is relocated, the movement is reported in increments to the host computer, which recalculates vector lists defining the B-spline surface and the net of lines connecting the vertices. If the vertex-connecting lines or B-spline surface are displayed while in the interactive modeling mode, some delay will be noted between the time of vertex movement completion and the corresponding change in the model. This delay is due to the time required for the host computer to communicate the updated vector lists to the PS 300. The delay will be about two to three seconds for update of the vertexconnecting lines and about ten seconds for update of the B-spline surface.

When the interactive modeling mode is activated, the label above the F7 key will read "PICK ROW." Pressing this key will alter the contral vertex selection function such that selections made with the stylus will affect an entire row or column of vertices at a time. The column or row is selected similarly to the selection of an individual vertex, except that the cursor is placed over one of the vertex-connecting lines in the row or column, instead of over the individual vertex. Iurning the vertex translation dials will then move the selected row or column of vertices in the desired direction while

retaining the orientation of the individual points within the row or column to each other. The user can return to selection of individual contral vertices by pressing the "PICK PI" (FB) key.

After moving a vertex it will occassionally be noticed that the vertex-cannecting lines will not quite reflect the new position of the vertex. Since the vertex movement is reported to the host computer incrementally, it is possible that a slight additional movement will trigger the update. At other times, a flaw in the communications between the host computer and the PS 300 causes an incremental change to be reported to the host as a very large or indecipherable movement. In that case, the distarted movement value is disregarded by the host program, which results in loss of the true incremental change. While there is no way to reconcile the difference between the contral vertex position as viewed on the screen and that held in the host computer's memory, it should be noted that the intersection of the vertexconnecting lines, and not the vertex cube, will indicate the true position upon which the B-spline surface will be calculated.
4.3.6 Input/output menu. The input/output menu is displayed in the function key labels when the $I / D$ (F10) key is pressed. The menu functions have not yet been implemented (with the exception of the F12 key), but when

implemented will offer the following options:
F1 PRI UERI prints a list of the current vertex locations and of the $B$ spline surface order selections.

F4 PLI SCRN plots a drawing of the model, as oriented and displayed on the screen, on the laser printer.

FB SAU UERT saves the current vertex location and surface order information to a disk file.

F9 LD UERI loads vertex location and surface order information from a disk File created with the SAU UERT Function.

F12 EXIT I/D returns the user to the main menu.

## CHAPIER 5

## MODELING TECHNIQUES AND CASE STUDIES

The B-spline modeling of sculptured surfaces greatly reduces the requirement for the more traditional techniques of surface development and representation reviewed in chapter 1. As was shown there, use of the traditional techniques requires that engineering and drafting skills be accompanied by an artistic touch in order to visualize and fair the surface in three dimensions. This ability is developed by the naval architect, and others who work often with sculptured surfaces, through years of experience and practice. On the other hand, while the B-spline techniques deemphasize the artistic requirement, it will still be necessary for the designer to develop an intuition for the placement of contral vertices which cannot be entirely reduced to a set of mathematical rules without sacrificing the control and flexibility of interactive modeling. The heuristic observations and case studies which follow are offered in order to facilitate the rapid acquisition of that intuition.

### 5.1. Modeling Iips and Techniques.

5.1.1. Known data. If the surface design is not to be developed ab initio, the preparation of a data file of known surface points will be essential. The selection of

such points for inclusion in this data file requires some consideration and advance planning. Primarily, the goal is to select sufficient points to accurately represent the form and boundaries of the surface, yet not so many as to create unnecessary clutter when the known data is displayed.

Two other considerations should be kept in mind during data point selection. First, the practicalities of displaying and visualizing the two surfaces which are to be matched (the known surface and the $B-s p l i n e ~ s u r f a c e ~ o r ~$ control graph) dictate that most of the modeling be performed while viewing two-dimensional sections cor very thin three-dimensional sections). This generally means locating control vertices nearly in the planes of known substructure data, such as the planes of a ship's transverse sections. Greater flexibility will be available in locating the control vertices for maximum surface control if the vertices' general locations are considered before finalizing the file of known surface data. Sections 5.1.3 and 5.1.4 will address the problem of vertex placement.

Secondly, if a symmetrical body such as a ship hull, automobile body, or airplane fuselage is being modeled, it will generally be easier if only one half of the structure is displayed, both of the known surface data and of the $B-$ spline surface and control graph. Modeling two identical

halves requires twice the manipulation as modeling a single half and results in much more difficulty interpreting the wire frame model due to ambiguities between lines in the foreground and those in the background. It is also virtually impossible to exactly duplicate the control graph for the halves of the body through a purely visual comparison. The only drawback to modeling a single half of a symmetrical body is that it is more difficult to ensure fairness at the juncture of the two halves. This problem can be remedied through use of the reflection display function, when that function is implemented.
5.1.2. Surface order. SPLINE offers the choice of two surface orders: third order or fourth order. The order may be specified independently in the $u$ and $w$ directions. As noted in chapter 2 , a fourth order curve produces the smoothest lines, but at the expense of some local control and the ability to easily effect sudden changes in curvature. It should also be remembered that a fourth order curve requires three coincident vertices for rows of vertices) to create a knuckle or chine, while the third order curve requires only two.

The third order surface will normally produce satisfactory results with the least amount of effort. The fourth order curve should be considered where smoothness of lines is an overriding constraint, such as in the
longitudinal lines of some ships and aircraft.
5.1.3. The control graph. Selection of the dimensions of the control graph (i.e., the number of vertices contained) is best accomplished by considering the locations where control points will be required for sufficient control of the surface. The most obvious considerations include:
(1) Uertices will be required to define the boundaries (ends and edges) of the surface.
(2) A vertex or row of vertices will generally be required at each maximum or minimum point.
(3) Particularly sharp curvatures or sudden changes in curvature will generally require two or more control vertices to achieve. Inflection points will require sufficient control vertices on each side of the point of inflection to establish curvature in opposite directions.
(4) Knuckles or hard chines will require two coincident rows of vertices in a third order surface or three coincident rows of vertices in a fourth order surface.
(5) While there is no constraint imposed by the B-spline algorithm nor by the computer program which would dictate that control



After the number of control vertices has been established, required manipulation of the vertices can be minimized by selecting a length-to-width ratio for the initial control graph which approximates that of the body to be modeled. This will be illustrated in the case studies which follow.
5.1.4. Control vertex placement. The approach to control vertex placement which was found to be most useful is to first locate the rows or columns of the control

graph in the desired plane and then to use the CLIP Function to compare an individual row or column of the control graph with the nearest substructure of the known surface data. In this way, most of the interactive modeling is performed in the more readily visualized twodimensional realm. Placing vertices is primarily a matter of keeping in mind the general properties of the B-spline, as innumerated in chapter 2 . Those properties are briefly reviewed below.
(1) The B-spline curve does not interpret the control polygon, but is contained within its convex hull, taken $K$ vertices at a time. This dictates locating the control vertices slightly outside of the curvature of the desired surface.
(2) The B-spline surface interpolates the corners of the control graph.
(3) While modeling is most efficiently performed in two dimensions, it must be kept in mind that the influence of each contral vertex is three-dimensional. This will occassionally require moving a vertex from its apparently proper position in two dimensions to accommodate some sudden change in the surface in the third dimension, or to avoid distorting the
surface by locating a vertex far from the plane of the remainder of its row or column in the control graph.
(4) The slope of the curve at the end points of the control polygon is determined by a straight line connecting the end point with the next point in the polygon. Again, the effect of vertices in the third dimension may cause unexpected deviations.
(5) A straight line is produced by $K$ collinear vertices.
(E) A curve tangent to the contral polygon is produce by $K-1$ collinear vertices.
(7) A knuckle is produce by $k-1$ coincident vertices.
5.1.5. Menu selections. The selection of display options from the menu can have a significant effect on the efficiency with which interactive modeling is performed. The requirement for displaying the control vertices is obvious, but it is useful to display the lines connecting the vertices of the control graph as well. Display of the connecting lines prevents confusion concerning the identity of a vertex in respect to its position in the contral graph matrix. If two points in a contral polygon are inadvertently interchanged, the result can be dramatic anomalies in the B-spline surface.

The CLIP function should be used as much as possible, since accurate depth perception is difficult with a wire frame model, even with depth cueing. This function is best disabled, however, when rotating the model. The RESET function is particularly useful for orienting the model for viewing sections in orthogonal planes with clipping.

While the object of the modeling is to mold a Bspline surface, most of the initial modeling is best performed without constant display of the surface. Display of the B-spline surface adds a profusion of lines to the already crowded screen display and slows response time considerably, since the host computer must communicate a new vector list for the surface to the PS 300 each time a vertex is moved. Due to the highly intuitive nature of B-spline manipulation, it is possible to achieve surprisingly accurate results by making the initial placement of control vertices without viewing the resulting surface at all. Due to the current limitations of the operating system, the images presented in the three case studies which follow were generated in this manner. Once the B-spline surface was initially displayed, further manipulation was not possible, as discussed in section 3.4. As will be seen, little further manipulation would be required for very accurate surface representation.
5.1.6. General procedure. The basic procedure for performing surface modeling with SPLINE can be summed up in a few steps.
(1) Preplan the initial placement of control graph rows and columns and select corresponding control graph dimensions.
(己) Do as much control vertex placement as possible by moving entire rows or columns of the control graph at a time.
(3) Use the CLIP function while modeling substructures in two dimensions, initially without display of the B-spline surface.
(4) After initial control vertex placement, view the entire contral graph in three dimensions. Ensure that the individual contral graph rows and columns do not have undesired extremes.
(5) Display the B-spline surface.
(6) Make minor adjustments to the control graph as needed.
5.2. Case Studu \#1: Modeling the Australia II

The first case study is a model of the hull of the sailing yacht, Australia II, excluding the famous winged keel. This case study illustrates the general approach to modeling a B-spline surface to an existing known surface or to preliminary design lines. The known surface data


Fig. 18. Lines drawing of the Australia II. Source:
Stannard $[24]$.
was extracted from a lines drawing (figure 1日) contained in Stannard's biography of Ben Lexcen [24].

Before entering SPLINE, the known surface data was put into a PREPS-Format file by digitizing it from the lines drawing with the two-dimensional digitizing program, DIGII. Iransverse sections were designated as substructures with about six to ten points each. Since the body plan presents the fore and aft section profiles on opposite sides of the $x z$ plane, it was necessary to manually modify the data file created by DIGII to place all half-section profiles on the same side of the plane. This was a simple matter of deleting minus signs from the data.

The final step before entering SPLINE was to determine the required contral graph dimensions. It was apparent that modeling would be performed most conveniently in two-dimensianal sections carresponding to substructures of the digitized data. Since the body shape was relatively uncomplicated in the body plan, it was decided to use anly five raws in the contral graph.

The longitudinal lines of the yacht required greater consideration. It will be useful to view figure 19, which shows the selected contral graph as squares connected by net lines and known surface points as unconnected asterisks, while examining the selection process which led to this control graph. The most easily selected locations


Fig 19. Initial control graph for Australia II, after relocating columns to known hull stations.
for columns of the control graph were a station at each end of the hull to, define those boundaries, and a station to define the maximum point of the keel. Since the shape of the forward sections is relatively uniform, two additional stations were expected to be sufficient to define the forebody.

The after half of the hull presented more interesting problems. The stern is not a U-shaped section, as most of the hull, but a U-shaped section. The stern also has a short portion which is somewhat elevated and very narrow, with nearly parallel sides. A second station was selected at the stern to help maintain the shape and size in that
region.
Between the keel and the stern, the transition from the U-section to the U-section is relatively abrupt, as can be seen in Eigure 20, which shows the two consecutive transverse sections. (Asterisks represent the known surface points.) A control graph column was selected for



#### Abstract

Fig. 20. Abrupt transition in the after hull of Austmalia II.


each of the illustrated sections, to define the approximate beginning and end of the transition region. It was expected that additional control would be required to ensure that the U-shaped station did not unduly influence the hull forward of the transition, nor the $U$ shaped section influence the shape aft of the transition.

The proximity of the two control graph columns selected for the stern was thought to be sufficient to maintain the shape between the U-shaped station aft of the transition and those at the stern. An additional U-shaped station was selected adjacent to the one located just forward of the transition, to minimize influence of the U-shaped stations forward of the transition. This made a final count of nine columns.

Upon entering SPLINE, a control graph size of (9,5) was selected, based on the above planning. The basis functions were defined as third order in both darections, and an initial control graph length-to-width ratio of eleven was chosen to roughly correspond to that of the


Fig. 21. Initial control graph for Austmaiza II.
hull. The resulting initial control graph can be seen in figure 21, along with the digitized known surface data.

Interactive modeling of the yacht hull was begun by selecting the ROW PICK function and moving the control graph columns into the selected positions, as shown in figure 19. The RESET function was then used to orient the hull for a bow view and the display was scaled to fill the screen. The CLIP function was then activated and the clipping window adjusted to a depth which allowed viewling the control vertices and known points of a single transverse station at a time (figure 22).

Individual transverse sections were modeled one at a


Fig. 2ᄅ. modeling.
time by selecting and moving the control vertices individually and moving the hull through the clipping window with the GLOBAL 2 dial to view each new station. All Five control vertices were located coincidentally at the bow. Figure 23 shows a more typical station with relocated vertices. Notice that the vertices are located slightly outside of the curvature of the known surface,
 hull of the control graph, but will not interpolate it. This offset is exaggerated in the illustration. The small tabs extending from the control vertices are the control graph lines which extend beyond the clipping window to vertices $1 n$ other control graph columns.


Fig. 23. Control polygon Ear a U-shaped station.

Figure 24 illustrates the contral polygon Ear a Ushaped section. The control vertices at the right are located above the bottom of the hull in order to remain outside of the curvature which occurs in the longitudinal direction (perpendicular to the screen). Three collinear vertices are used to define the flat bottom between the two right-hand points, as well as the slope of the bottom as it begins the upward curvature between the second and third collinear vertices.


Fig. 24. Control polygon for a U-shaped section. The final control graph is pictured in figure 25. Notice that the net of lines is uniform in both the transverse and longitudinal directians. The resulting Bspline surface is shown in figure $2 E$ with the known


Fig. 25. Final control graph for Australia II.

surface points for comparison. The match is generally quite good, but an additional control graph column is needed near the bow to hold the keel line downward. A claser view of the transition fram U-shaped to U-shaped sections is shown in Eigure 27, which depicts the B-spline surface and its associated contral graph.


Fig. 27. B-spline model of Austmalia II stern.
The next step in modeling the hull would be to again view the transverse stations one at a time and make minor adjustments in the contral graph. Figure 28 campares the control vertices (squares), known surface (asterisks) and B-spline surface (salid line) for a U-shaped station. It can be seen that only very minor adjustments are indicated.


Fig. 28. B-spline surface at a U-shaped station.


Fig. 29. B-spline surface at a U-shaped station.

Figure 29 shows the B-spline surface achieved at a Ushaped section and illustrates one of the pitfalls of considering primarily two-dimensional sections while modeling a three-dimensional surface. The three collinear vertices at the bottom would dictate a straight line in the right-hand segment of the B-spline curve in two dimensions. However, the surface is pulled downward at the right-hand edge by the effects of the vertices at stations located further forward. A considerable upward adjustment of the right-hand control vertex may be necessary to overcome this pull from other stations. 5.3. Case Study \#2: Modeling a Porsche 944

The second case study involves very similar considerations to the first and will be presented more briefly. The body of a Porsche 944 automobile was modeled, reemphasizing the techniques discussed previously and illustrating the versatility of the B-spline and of SPLINE.

The known surface data for the Porsche was approximated by digitizing points from a lines drawing and profile contained in advertising literature. Once again, DIGII was used to create the data file. The data for half of the symmetrical body was presented to SPLINE without reflection.

The shape of the surface was considered in order to estimate the required dimensions of the control graph.


Fig. 30. Initial control graph column locations fcr Porsche 944 body.


Figures 30 and 31 illustrate the selection of transverse stations for modeling, similar to those chosen for the previous case study. In this case, the control graph is presented in an edge view. Looking first at the longitudinal lines, it was determined that ten control graph columns would be required. A station was selected at each end, another near the front cto avoid the problem encountered in modeling the bow of the Australia IIJ, and a station near the middle at the point of maximum height in the profile. Two stations were determined to be necessary to achieve the small-radius curvature at the base of the windshield, and two more at the top. Finally, two intermediate stations were positioned in the rear half of the body. If an eleventh station had been available, it would have been place midway along the hood of the automobile.

With consideration to the shape of the transverse sections, seven control graph rows were deemed necessary. Figure 32 depicts a section across the hood being modeled and illustrates the reason for selection of seven control graph rows. Since the sharp curvatures and sudden transitions in the body dictated use of a B-spline which was third order in both dimensions, three vertices were required to achieve the nearly flat hood and roof of the automobile, with an additional vertex at the hard chine between the hood and fender. (The brighter vertex seen
there vertices mold the curve at the side of the automobile.


Fig. 32. Modeling a forebody section of a Porsche 944.
As detailed previously in case study \#1, interactive modeling was performed by first moving control graph columns to the selected stations, then modeling individual transverse stations with clipping enabled. Examining the contral vertices of figure 32 from right to left, the first three vertices are placed nearly linearly to give the nearly flat surface of the hood. The third and fourth vertices are placed at the same point to achieve the knuckle. The fifth vertex serves two functions. The control polygon line connecting this vertex with the vertices at the knuckle defines the slope of the curve as
it flows downward from the knuckle. The position of the Fifth and sixth vertices define the maximum for the curve in the fender. Finally, the last vertex defines the lower boundary of the surface.


Fig. 33. Control graph and known surface for a Porsche 944.

Figure 33 presents the final control graph after modeling the individual sections, along with the known surface data. While each individual station appeared to be adequately modeled, displaying the control graph lines (figure 34) revealed a problem. Near the midsection of the automobile, one vertex was placed much lower on the body's contour than the corresponding vertices in adjacent columns. While the placement had appeared adequate when


Fig. 34. Control graph for Porsche 944 with an inconsistency in one raw at the midsection.


Fig. 35. B-spline representation of a Porsche 944.

viewed in the transverse plane, it was now apparent that this vertex was sharply out of position when viewed as part of its control graph row.

The effect of this placement can be seen in figure 35. Much of the apparent distortion in the body at the midsection is only an illusion caused by the manner in Which the net of lines representing the B-spline surface is displayed. Some real distortion does also occur in this region due to the added pull of the misplaced vertex. Ihis case study illustrates well the importance of considering and reviewing the control graph in three dimensions.

Figures 36 and 37 present comparisons of the B-spline


Fig. 3E. B-spline surface with a hard chine.


Fig. 37. B-spline representation of a Porsche surface. surface to the contral vertices and known surface points. Note that the two coincident vertices in figure 36 produce a hard chine, while placing the vertices slightly apart, as in figure 37, produces a small-radius curvature.

The effect on this station of control vertices at other stations can again be seen in figure 36, where the surface of the hood is pulled up from the desired form by the control vertices at the next station, which are located higher for the windshield. Figure 37 also illustrates the remarkably accurate surface which can be abtained even without viewing the B-spline surface during initial control graph arrangement.


### 5.4. Case Studu \#3: Freeform Modeling

The final case study presents an example of freeform modeling, in this case of a Stetson hat. In ab initio design, the engineer often has a general idea of the form which he or she is trying to achieve, but is not constrained by a requirement to exactly match previously existing lines. For this reason, no attempt was made to compare this model to a preexisting design.

In the absence of such previous form definition, it will often be beneficial for the designer to sketch a few basic lines to aid in visualizing the shape and the required control graph dimensions. Because of the difficulty in visualization of the more abstract form, in this particular case it was also found to be useful to model both halves of the object, even though it is symmetrical.

Aside from these initial considerations, the modeling approach is basically the same as that in the first two case studies. A third order B-spline was used with a seven by seven contral vertex matrix, based on form considerations which will become apparent as the model development is reviewed. A length to width ratio of 1.3 was selected. Figure 38 presents the initial control graph.

Uiewing the planar control graph as being in the horizontal plane of the hat's brim, vertices defining the


Fig. 38. Initial control graph for a Stetson hat.


Fig. 39. Control graph rows and columns relocated.
sides of the crown were to require placement nearly vertically above one another. For this reason, the ROW PICK feature was used to relocate rows and calumns of the contral graph as shown in Eigure 39. Natice that the secand calumn fram the right exhibits the disparity between contral vertex position and contral graph line position which was discussed at the end of section 4.3.5. When moving the calumn of contral vertices, one increment of the movement was distorted during communication between the twa computers and thus ignared by the hast computer's program. In all subsequent operations, there will continue to be a disparity between the position of these vertices as displayed by the PS 300 and as used in the preparation of vector lists and calculation of surfaces by the host computer. The intersection of the contral graph lines, and not the individual cubes, marks the vertex position upon which the B-spline surface will be based.

After positioning individual vertices to define the rounded shape of the surface edges (figure 40), the vertices controlling the surface of the hat's crown were pulled up from the surface. To achieve uniformity of the similar halves, the points were first selected with the stylus while the contral graph was in an orientation similar to that shown in figure 41 , then the display was rotated to present an edge view (Figure 42) before the selected vertices were moved. Also in the interest of


Fig. 40. Surface edge boundaries established.


Fig. 41. Elevated vertices define crown.
achieving uniformity, the modeling was performed without use of the CLIP function, allowing direct comparisons to be made between foreground and background lines. Notice the depth cueing in the right rear quadrant of figure 41 which gives the viewer a better perception of the display orientation.


Fig. 42. Elevating the brim.
The final step in forming the contral graph was to elevate the first and last rows of the control graph to achleve the raised brim (Figure 42). It was possible to do this very easily in the ROW PICK mode, even though points in the rows had been moved around to accomplish the rounding of the edges of the brim. The entire row of vertices could be moved simultaneously without affecting
the relative pasition of the individual vertices in the row to each other.


Fig. 43. Stetson hat with control graph.
Figure 43 presents the final control graph of the hat with the resulting B-spline surface. Notice that while the vertices form a relatively rounded brim (Eigure 40), the resulting surface has distinct corners (figure 43). This effect is due to the fact that only the corner vertices of the control graph are interpolated by the surface. Since the adjacent vertices are not interpolated, the result is a sharp discontinuity at each of the four corners of the control graph. In order to present the desired smooth boundary, these four vertices must be relocated to lie on the intended edge of the
surface, rather than on a smooth curve connecting the adjacent vertices.

While the hat perhaps belongs more correctly on Huckleberry Finn's head than on a cowboy's, it nevertheless illustrates well the great potential for Freeform design with surface B-splines. Figure 44 presents a section view of the same hat and control graph.


Fig. 44. Section view of hat with control polygon.

## RECDMMENDAIIDNS AND CDNCLUSIDNS

### 6.1. Hardware and Firmware Modifications

Several modifications to the hardware and firmware of the system upon which SPLINE was developed would significantly enhance the program. At this time the University of Washington Mechanical Engineering Department's PDP-11 computer is being replaced by a UAX11/750. This replacement makes possible most of the enhancements discussed below.
6.1.1. High-speed interface. It was initially planned that SPLINE would make use of rubber sheeting, the real-time modification of the B-spline surface display in response to control vertex manipulations. However, it soon became apparent that communication between the two computers, at 9600 baud, was far too slow to effect realtime response.

Rogers and Satterfield [17] found calculation of the Full B-spline algorithm too slow to allow surface dragging or rubber sheeting, so developed an abbreviated algorithm which took into effect the localized effect of a single contral vertex movement. Using the present system, even the time for a full B-spline surface calculation was found to be insignificant compared to the time required to communicate a new vector list, however calculated, to the


PS 300. It takes approximately ten seconds for the host computer to send the vector list for the B-spline surface.

The PS 300 manual [20] states, "This interface is best suited for infrequent communication of small amounts of data." The interface simply is not designed to support a program such as SPLINE. Upgrading the system with Evans and Sutherland's 56 kilobaud high-speed interface would provide a distinct improvement in the program operation.
6.1.2. UAX host computer. The greatest potential benefit of interfacing the PS 300 with the newly installed UAX computer is avoidance of the PDP-11 operating system discrepancies. It is expected that SPLINE wauld require Few madifications to compile on the UAX system.
6.1.3. Graphics Support Routines. A totally different host-resident communications software package is available for the PS 300 on UAX systems than is used on the PDP-11. The Graphics Support Routines provide significantly more reliable communications between the host computer and the PS 300. Additionally, these routines perform same prepracessing of data in the host CPU, resulting in substantially faster communications. Upgrading the system with the Graphics Support Routines would require some revision of the manner in which SPLINE presents data for communication to the PS 300, but wauld provide a worthwhile enhancement.

## E.2. Program Expansions

SPLINE was designed to support many features which are not yet fully implemented. For many of these features, the PS 300-resident portion of the program already includes the necessary statements to handle display and selection of the additional options. The programs are carefully documented to facilitate expansion. 6.2.1. Input/output menu selections. The first program expansion which should be investigated is the implementation of all input/output menu selections. At the present time the function key presses are reported to the FORTRAN subroutine, 10 . However only a shell of the subroutine exists and is totally nonfunctional.

The most needed output ability is that to print the final control vertex positions on disk or paper. The primary purpose of the program is actually to obtain such a listing, the control vertex positions being an integral part of the B-spline algorithm which defines the modeled surface. Such a listing should include the order of the surface, the homogeneous coordinates, and the knot vectors. These values are readily available and identified within SPLINE.FIN the FORTRAN portion of SPLINE 3 and interfacing with the printer should be relatively straightforward.

The variable, KEY, in subroutine 10 is equal to the number of the function key which was pressed.

The next input/output menu functions which need to be implemented are the saving to disk and loading from disk of control vertex positions, allowing work in progress to be saved and restarted later at the point from which it was saved. This task will be very similar to that of implementing the print function, except that some effort may be required to avoid having contral vertex manipulations for the currently displayed model apply to a new set of vertices when loaded from a disk file.

The most difficult input/output menu option to implement may be the plot function, intended as a screen dump. While the host program is aware of current vertex locations relative to one another, it is not informed of rotations, scaling, global translations, and clipping which are performed by the PS 300. Even if this information were communicated to the FORIRAN program, the programming required to accomplish the matrix transformations in the host-resident program would be sobering. The PS 300 programming language has a function called XFORMDATA, however, which retrieves the transformed data for an object as ASCII data for transmission to the host computer. Using this function, it should be possible to implement a screen dump function without excessive difficulty.
6.2.2. Inversion algorithm. The time required to model a desired surface could be greatly reduce with the
implementation of an inversion algorithm. Such an algorithm would calculate an initial set of control vertex positions, the required surface order, the homogeneous coordinates and the knot vectors which would yield a Bspline surface approximating the surface represented by data in the known-surface data file. The program would branch to such a subroutine almost immediately after program execution, from subroutine INITCP.

Because the B-spline surface does not interpolate the control vertices, developing and implementing a suitable inversion procedure is not a trivial task. Iwodimensional approaches to the problem are presented by Yamaguchi [25] and Wu, Abel, and Greenberg [21]. A more complex (but more immediately applicable) threedimensional algorithm is presented by Barsky and Greenberg [12,26]. Rogers, Satterfield, and Rodriguez offer yet another three-dimensional approach [6,17], which they describe as "conceptually simpler, but computationally less efficient" than Barsky and Greenberg's. They offer as justification a reminder that the inversion algorithm is used only once during the program, to obtain an initial approximation. Tiller [18] presents some thoughts relevant to approximating surfaces with nonuniform rational B-splines.

It should not be assumed that an inversion algorithm will render interactive modeling obsolete. The algorithm
offered by Rogers, Satterfield, and Rodriguez, for example, does not automatically create hard chines, which must then be added interactively. Even if an inversion algorithm was capable of yielding a B-spline surface which exactly interpolated the known surface data, some interactive manipulation would be required to make the surface suitable. Digitized data from a sculpted surface is almost never fair, having small oscillations due to the digitization process. These oscillations must be removed either by extensive and difficult preprocessing of the data or through interactive manipulation.
6.2.3. Circular arcs. Consideration of Iiller's work with the representation of circular arcs by nonuniform rational B-splines suggests an additional feature useful during interactive modeling. With a suitable inversion algorithm, the user cauld place several contral vertices under program control, identify three paints on a desired circular arc, and allow the program to relocate the vertices to yield a circular arc interpolating the three points. Since the manipulation of homogeneous coordinates and of nonuniform knot spacing is not highly intuitive, such an approach is necessary in order to make use of the power of the nonuniform rational B-spline.
E.2.4. Orthogonal plane intersection mapping. The parametric representation of the surface presented by SPLINE is adequate for accurate visualization of the $B-$

spline surface. For some applications, however, a more traditional representation of waterlines, buttocks lines, and transverse sections is desirable. In order to implement such a display, it is necessary to map the intersection of the B-spline surface with the three basic orthogonal planes.

The PS 300-resident portion of SPLINE, SPLINE.DAT, already has the necessary structure to display the three intersection maps. SPLINE.FIN would have to present the vector lists to the PS 300 with a command of the format:
XY:=UECTOR_LIST ITEMIZED N= . . . .

The vector list would be fallowed by the sending of an appropriate value to the PS 300 program variable, XYMODE, and the sending of a triggering message to input number one of NEW_MODE. The communication of control graph vector lists in subroutine CPLINE provides a similar example.

Calculation of the vector list should be implemented in subroutine PLANES, which is currently called from subroutine WAIT when the appropriate function key is pressed.

Mapping of the intersection between the planes and the $B$-spline surface can be difficult, especially when trying to obtain sufficient accuracy for an adequate display. Multiple disconnected contours, such as contours of adjacent peaks, present a particular problem.

Heap [27] presents three algorithms for the production of contour maps of a function defined at the vertices of an irregular triangular mesh. Such a mesh is often used in finite element techniques, particularly for the solution of partial differential equations. Heap's algorithm first creates the triangular mesh, with vertices of the mesh lying on the surface to be mapped. The algorithm then follows the contour from element to element of the mesh. Since straight lines are generated through each mesh element, a very fine mesh is required for an accurate contour, consuming large amounts of memory. SPLINE already approaches the memory limit of the POP11.

Satterfield and Rogers [2日] suggest using Heap's algorithm to obtain a triangular mesh along the path of the contour, but then present a variation. They use the triangular mesh as a basis for piecewise B-spline calculation of the surface in the region of the mesh. Pairs of surface points separated by a desired tolerance are generated on the B-spline surface and checked for spanning of the contour. When they are found to span the contour, a more exact contaur lacation is determined by interpolating between the two spanning points. This procedure handles properly the problems of correctly ordering the points of a contour and of multiple disconnected contours in a single contour plane.
2


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6.2.5. Reflection about a plane. Like the orthogonal plane intersection mapping, display of a reflection of the model about a plane has been fully implemented in SPLINE.DAT, but remains to be implemented in SPLINE.FTN. Calculation of the vectar list would be trivial, requiring only that an affset be added to ar deducted fram the appropriate vector information already held in memory. Communication of the vector infarmatian wauld be similar to that detailed in section 6.2.4, above. Pressing the appropriate function key already activates a call to subrautine REFLECT.
E.2.E. Calculation of Eorm parameters. The mathematical nature of the surface representation could be made even more useful with automatic calculation of form parameters, such as center of gravity, section areas, or waterplane area. No provision has been made in SPLINE at this time for such a feature. Cruetz and Schubert [29] take this approach one step further yet. They propose allowing the designer to specify initial form parameters, such as a section area curve, block coefficient, and beam to draft ratio, and letting the computer program generate From that an initial body plan.


### 6.3. Conclusions

SPLINE has demonstrated the tremendous potential which exists for mathematical definition of sculptured surfaces coupled with highly interactive computer
$=1$
graphics. Dramatic changes in the efficiency with which automobile bodies, aircraft fuselages, and ship hulls are designed and manufactured can be expected in the very near future. Using B-splines, or similar mathematical representations, the definition of a complex sculptured surface will take hours, not days. Modifications to a developed surface will be accomplished in mere minutes, no longer requiring the designer to essentially start over with calculations and fairing of lines.

Not only will surface definitions be achieved more accurately and efficiently, but those definitions will be directly interfaced with computer programs which will avaluate the performance characteristics of the form and with the machinery which will manufacture it. Further effort in the development of accurate inversion algorithms, in user/computer interfacing, and in generation of form parameters from surface definitions will be particularly important.
and

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$$
\begin{gathered}
\text { APPENDIX A } \\
\text { FLOW CHARTS AND FUNCIION NETWORKS }
\end{gathered}
$$

The figures contained in this appendix present flow charts and function networks for the major program functions of both SPLINE.FIN (the host-resident program) and SPLINE.DAI (the PS 300-resident program). The pragram listings are given in appendices $B$ and $C . \quad$ The comments contained in those listings will be particularly useful in understanding the function netwarks. Those who are unfamiliar with the PS 300 programming language will want to consult the computer manual [20] for an explanation of display trees and function networking and for details concerning the individual function blocks.


Fig. 45. SPLINE.FIN flow chart.


Fig. 46. SPLINE.DAI display tree.

## ROTATION



Fig. 47. Rotation function netwark.


## SCAL ING



Fig. 48. Scaling function network.


Fig. 49. Typical function network for function key mode selection and labeling.


Fig. 50. Function network for blinking of translation dials when in interactive modeling mode.


Fig. 51. Clipping Function network.

## PICKING



Fig. 52. Picking function network.

## CONVERT PICKID TO INTEGER





Fig. 54. Function network for global translation and translation of selected vertex during interactive modeling.


Fig. 55. Function netwark for reparting of vertex movement to FORTRAN pragram.


Fig. S5. Function network to reset vertex movement accumulator when new vertex is picked.

# APPENDIX B <br> SPLINE.FIN PROGRAM LISIING 

SPLINE.FIN is the host-resident portion of the program, SPLINE.

```
*************************************************************
******************* Program SPLINE.FIN *******************
```



```
***********************************************************
*
*Input :
*Output : *
*Cal1s : INITPS, PSEXIT,INITCP,WAIT *
*Alters : *
*Description: This program facilitates three-dimensional *
*
*
*
*
*
*
*
*
*Author: 
*Author: : D. Michael Bryant *
*Created On : 5/21/87 Modified Dn: *
*
surface modeling or design using a surface *
B-spline algorithm. The surface is displayed*
and interactively manipulated and modified *
in real time on the PS-300 vector refresh *
display. The Eile, "SPLINE.DAT," contains *
the PS-300 command language program which *
produces and controls the graphics display *
using data supplied by SPLINE.FIN. *
* *
***********************************************************
*Uariable Iype Explanation *
*-------- ------- ------------ *
*ISIAT(1) Integer Reports error status from PS-300 *
***********************************************************
```


## PROGRAM SPLINE

CDMMUN /SPLINE/ MCP, NCP, CP(10, 8,4$)$, MORDER, NDRDER CDMMDN /BASIS/ R(13,4,31), S(11,4,31), SURF(3,31,31) COMMDN /UECS/ UECS(1000)
DIMENSION ISTAT(1)
***** Send PS-300 command language program to PS-300 and ***** execute.

CALL INITPS
***** Establish initial control point locations.
CALL INITCP
***** Await and act upon signals from PS-300 program.
CALL WAIT
***** De-establish link between PS-300 and PDP-11, using
***** library subroutine.
ISTAT (1) =0
CALL PSEXIT(1,ISTAT)
STOP
END
******** Subroutines Follow in Alphabetical Order *********
********************************************************** ***********************************************************

Subrautine BLANK w********************

 *

* Input : I , BUFFER *
*Output : BUFFER *
*Calls : *
*Alters : BUFFER *
*Description: Ihis program makes extensive use of the *
* 'ENCODE' command to convert integers to *
* characters in a LOGICAL*1 array ('BUFFER'). *
* The buffer is then passes to the PS-300, *
* with the encoded integers forming partions
* of the names of nodes, I.E. 'CP23'. When a *
* single-digit integer is encoded with an 'I己'*
* specification, however, the result is not *
* '03', far example, but ' 3'. The blank *
* 
* 
* 

*Authar : D. Michael Bryant
*Created On : 11/17/86
Modified On:
*
would not be allowed as part of a node name.* Ihis subrautine replaces the unwanted blanks* with "O's".
 *
*Uariable Iype Explanation *
*-------- ------- ----------- * *

IF (BUFFER(I).EQ.' ') BLFFER(I)='O'

REIURN
END


## *********************************************************

 ******************** Subroutine BSPLIN


SUBROUTINE BSPLIN
CDMMON /SPLINE/ MCP, NCP, CP(10, B, 4), MORDER, NORDER COMMDN /BASIS/ R(13,4,31), S(11,4,31), $\operatorname{SURF}(3,31,31)$ DIMENSION UKNDI (15), UKNDT(13), U(31), W(31)

Blink "B-SPLINE" label on keyboard while calculating.
CALL PSSEND (24,'SEND IRUE ID <2>FLABEL己;')
CALL PSSEND (22,'SEND 1 IO <1>NEW_MODE;')
Determine knot vectors (default = uniform).
UMAX $=$ REAL (MCP-MORDER +1 )
WMAX $=$ REAL (NCP-NDRDER +1 )

DD $150 \mathrm{~K}=1$, MCP + MORDER
IF (K.LE.MORDER) UKNDT (K)=0.O
IF (K.GT.MDRDER.AND.K.LE.MCP) UKNDI(K) = $\operatorname{UKNOI}(K-1)+1.0$
IF (K.GI.MCP) UKNDT (K) $=$ UMAX

DO $160 K=1$ ，NCP＋NORDER
IF（K．LE．NORDER）WKNOT（K）$=0.0$
IF（K．GI．NORDER．AND．K．LE．NCP）WKNOT（K）＝ WKNDI（K－1）＋1．0
IF（K．GT．NCP）WKNDT（K）$=$ WMAX
160 CONIINUE
＊＊＊＊＊Determine parametric spacing of displayed B－spline surface net lines．

UINC $=$ UMAX／30．0
WINC $=$ WMAX／30．0
n0 200 K＝1，31
$U(K)=(R E A L(K-1)) * U I N C$
$W(K)=(R E A L(K-1)) * W I N C$
200 CONTINUE
Determine first order basis functions．
Dロ 250 M $=1$, MCP + MORDER－1
DO $240 \mathrm{~K}=1,31$
IF（UKNQI（M）．LE．U（K）．AND．U（K）．LI．UKNOI（M＋1）） THEN
$R(M, 1, K)=1.0$
ELSEIF（UKNQT（M）．EQ．U（K））THEN
$R(M, 1, K)=1.0$
ELSEIF（K．EQ．31．AND．M．EQ．MCP）THEN
$R(M, 1, K)=1.0$
ELSE
$R(M, 1, K)=0.0$
ENDIF
240 CONTINUE
250 CONTINUE
Dロ $270 \mathrm{~N}=1, \mathrm{NCP}+\mathrm{NORDER}-1$
पロ 260 K＝1，31
IF（WKNDI（N）．LE．W（K）．AND．W（K）．LI．WKNDI（N＋1））
IHEN
$S(N, 1, K)=1.0$
ELSEIF（WKNOI（N）．EQ．W（K））THEN
$S(N, 1, K)=1.0$
ELSEIF（K．EQ． $31 . A N D . N . E Q . N C P)$ THEN
$S(N, 1, K)=1.0$
ELSE
$S(N, 1, K)=0.0$
ENDIF
CONTINUE
260
270
CONTINUE

Calculate higher order basis functions.

```
DO 350 K = 2,MORDER
    DO 340 M = 1,MCP+MORDER-K
                DO 330 I = 1,31
```

                                \(A=U K N D I(M+K-1)-U K N D I(M)\)
                                IF (A.EQ.O.O) THEN
                            \(B=0.0\)
                ELSE
                            \(B=(U(I)-U K N D I(M)) * R(M, K-1, I) / A\)
                ENDIF
                C = UKNOI (M+K) - UKNDI (M+1)
                    IF (C.EQ.O.O) THEN
                        \(D=0.0\)
                    ELSE
                        \(D=(U K N O I(M+K)-U(I)) * R(M+1, K-1, I) / C\)
                    ENDIF
    $$
R(M, K, I)=B+D
$$

CONTINUE
CONTINUE

DO $450 \mathrm{~K}=2$, NORDER
DO $440 \mathrm{~N}=1, N C P+N O R D E R-K$
DO $430 \mathrm{I}=1,31$
$A=W K N D T(N+K-1)-W K N Q I(N)$
IF (A.EQ.O.O) THEN
$B=0.0$
ELSE
$B=(W(I)-W \operatorname{KNOI}(N)) * S(N, K-1, I) / A$
ENDIF
$C=W K N Q I(N+K)-W K N Q I(N+1)$
IF (C.EQ.O.O) THEN
$D=0.0$
ELSE
$D=(W \operatorname{NNOT}(N+K)-W(I)) * S(N+1, K-1, I) / C$ ENDIF
$S(N, K, I)=B+D$
CONIINUE
CONTINUE
CONTINUE

Calculate the surface coordinates.

```
    OO BOO I = 1,MCP
        00 790 J = 1,NCP
        DO 7BO L = 1,31
                            IF (R(I,MORDER,L).EQ.O.O) GOID 7BO
                            DO 770 M = 1,31
                            IF(SCJ,NORDER,M).ED.O.O) GOID 770
            0O 760 K = 1,3
                                    SURF(K,L,M) = SURF(K,L,M) +
                                    CP(I,J,K) *
                                    CP(I,J,4) *
                                    R(I,MORDER,L)*
                                    S(J,NORDER,M)

CALL SURFAC

\section*{Stop blinking "B-SPLINE" label on keyboard.}

CALL PSSEND (25,'SEND FALSE ID <2>FLABEL2;')
CALL PSSEND (22,'SEND 1 TD < 1>NEW_MODE;')
REIURN
END


\section*{SUBROUTINE CPLINE}

COMMDN /UECS/ UECS(1000)
LOGICAL LP(333)
CDMMON /SPLINE/ MCP,NCP,CP(10, B, 4), MORDER, NORDER LOGICAL* 1 BUFFER(8O)

I UEC=0
ILP=O
Vector list for lines along rows of vertices.
DO \(100 \mathrm{M}=1\), MCP
DO \(90 \mathrm{~N}=1\), NCP
Count the vectors created.
ILP=ILP+1
DO 80 I=1,3
Count the vector components \((X, Y, Z)\) created.
IUEC = IUEC + 1
UECS (IUEC) \(=C P(M, N, I)\)
80 CDNIINUE

Indicate whether vector is point or line vector.
```

LP(ILP) = .IRUE.
IF (N.EQ.1) LP(ILP) = .FALSE.

```

CONTINUE
CONIINUE
Vector list for lines along columns of vertices.
DO \(200 \mathrm{~N}=1\), NCP
DO \(190 \mathrm{M}=1\), MCP
\(I L P=I L P+1\)
DO \(180 \mathrm{I}=1,3\) IUEC = IUEC + 1 UECS (IUEC) \(=\operatorname{CP}(M, N, I)\) CDNTINUE

Indicate whether vector is point or line vector.
```

LP(ILP) = .IRUE.
IF (M.EQ.1) LP(ILP) = .FALSE.

```

Send vector list to PS-300 program to define

ENCODE ( \(31,210, B L F F E R\) ) ILP
210
FORMAI ('CPL:=UECIOR_LISI IIEMIZED N=', I3)
CALL PSSEND ( \(31, B L F F E R\) )
CALL PSUECS ( 4, ILP, UECS, LP, .IRUE., IOSTAT)
REIURN
END



SUBROUIINE INITCP
COMMDN /SPLINE/ MCP, NCP, \(\operatorname{CP}(10,8,4)\), MORDER, NORDER CHARACIER*1 ANSWER LOGICAL*1 BUFFER (80)

Determine whether it is desired to display a known surface.

50 TYPE 60
60 FORMAI(///,' Do you wish to display a known
\(+\quad\) 'surface from a PREPS-format file?',,
+ , Please answer (Y) or ( \(N\) ).', /)
READ(5,70,ERR=50) ANSWER
IF (ANSWER.EQ.'Y') GOID 100 IF (ANSWER.EQ.'N') GOTD 200 GOTD 50

Allow input of coordinates of points on a known surface from a PREPS-format file.

100 CALL PREPS
Establish size and length/width ratio of initial
contral point matrix.
200 TYPE 201
201 FORMAT(//' A matrix of vertices up to (10 X 8)',
\begin{tabular}{|c|c|c|}
\hline + & & may be \\
\hline + & & ENTER THE DESIRED \\
\hline + & & (Number of tr \\
\hline + & & stations.)', /, \\
\hline + & & Example: 7,5',1) \\
\hline
\end{tabular}

210 READ (5, *, ERR=200) MCP, NCP
IF (MCP.GT.10.OR.NCP.GT.8) THEN
TYPE 220
220 FORMAT (/,' The maximum value for the', matrix is 10,8.'/, ENTER BOTH UALUES AGAIN.')
GOTD 210
ELSEIF (MCP.LT.5.OR.NCP.LT.5) THEN
TYPE 230
230
FORMAI (/,' The minimum value for the', matrix is 5,5.'/,
\(+\)
GOTD 210
ENDIF

235 TYPE 240
240 FORMAT(///,' Enter the desired length/width ',/, ratio for the vertices matrix.',/

READ (5,*,ERR=235) RATID
IF (RATIO.LE.O) THEN
TYPE 250
250 FORMATC/,' THE LENGTH/WIDIH RATID MUST',
GOTD 235

\section*{ENDIF}
***** Determine the order of the B-spline surface equation.
TYPE 265
```

265
FORMAT (//,' Enter the order of the B-spline',/,
+ ' surface in the longitudinal direction.')
270 TYPE 275
275 FORMAT (' Use integer values of 3 or 4.')
READ (5,*,ERR=270) MORDER
IF (MORDER.LT.3.OR.MORDER.GT.4) GOTD 270
TYPE 280
280 FORMAT (//,' Enter the order of the B-spline',/,
285 TYPE 275
READ (5,*,ERR=2B5) NDRDER
IF (NORDER.LT.3.OR.NORDER.GI.4) GOTD 285

```

Calculate the coordinates of the initial vertices matrix.

Determine the \(X\) and \(Y\) spacing of the vertices.
DM=1.0/FLOAT(MCP-1)
IF (NCP.EQ.1) THEN
\(\mathrm{DN}=0.0\)
ELSE
\(\mathrm{DN}=1.0 /(\) RAT ID*FLDAT(NCP-1) )
ENDIF
Calculate the coordinates.
\[
\text { YMIN }=0.0-1.0 /(\text { RATIO*2.0) }
\]

D 310 M=1, MCP
DO \(300 \mathrm{~N}=1\), NCP
\(\operatorname{CP}(M, N, 1)=-0.5+\operatorname{FLOAT}(M-1) *\) M
\(C P(M, N, Z)=Y M I N+F L O A I(N-1) * D N\)
\(C P(M, N, 3)=0.0\)
\(\operatorname{CP}(M, N, 4)=1.0\)
* Default homogeneous coordinate = 1 for

Send the necessary program lines to the PS-300 to
***** display the vertices correctly positioned.

\section*{500 CONTINUE}

DO 700 M \(=1\), MCP DO \(690 \mathrm{~N}=1, \mathrm{NCP}\)

NUMCP \(=\mathrm{M}+(\mathrm{N}-1)\) *10
ENCDDE (50,510, BUFFER) NUMCP, NUMCP

510

520

530

540

545

FORMAT ('CP', I2,':=BEGIN STRUCTURE SET',
PICKING IDENTIFIER=CP', I2,';'
CALL BLANK ( \(3, B \cup F F E R\) )
CALL BLANK(4日,BUFFER)
CALL PSSEND(50,BUFFER)
CALL PSSEND (25,'TRAN:=TRANSLATE BY 0,0,0;')
CALL PSSEND (17,'INSTANCE OF CUBE;')
CALL PSSEND (14,'END_STRUCTURE;')
ENCODE (28,520, BUFFER) NUMCP
FORMAT ('TRAN_TOTAL_', I2,':=F:', 'aCCUMULATE;')
CALL BLANK(12, BUFFER)
CALL PSSEND (2B, BUFFER)
ENCODE (38,530, BUFFER) NUMCP, NUMCP
FORMAT ('CDNNECT TRAN_TOTAL_',I2,
'<1>:<1>CP', I2,'.TRAN;')
CALL BLANK(20,BUFFER)
CALL BLANK (31, BUFFER)
CALL PSSEND (38, BUFFER)
ENCODE (52,540,BUFFER) CP(M,N,1), CP(M,N,2), CP(M, N, 3), NUMCP
FORMAT ('SEND UC',F7.4,',',F7.4,',', F7.4,') TO <2>IRAN_TOTAL_', I2,';'>
CALL BLANK (50, BUFFER)
CALL PSSEND (52, BUFFER)
ENCODE ( 34,545, BUFFER) NUMCP
FORMAT ('SEND U(O,O,O) ID', <1>IRAN IOTAL_',I2,';'
CALL BLANK (32, BUFFER)
CALL PSSEND (34, BUFFER)


\section*{ENCODE（28，550，BUFFER）NUMCP}

FORMAI（＇SEND ． 1 TD＜4＞IRAN＿TOTAL＿＇，I2，
CALL BLANK（26，BUFFER）
CALL PSSEND（2日，BUFFER）
ENCODE（41，560，BUFFER）NUMCP，NUMCP
FORMAT（＇CDNNECT SWITCH＿PICKく＇，I2， ＇＞：＜1＞IRAN＿IロTAL＿＇，I2，＇；＇）
CALL BLANK（21，BUFFER）
CALL BLANK（39，BUFFER）
CALL PSSEND（ 41, BUFFER）
Connect the dial signal to the switch outputs for row ＊＊＊＊＊and column movement．

\author{
ENCODE（41，560，BUFFER）M＋80，NUMCP \\ CALL BLANK（39，BUFFER） \\ CALL PSSEND（ 41, BUFFER） \\ ENCDDE（ 41,560, BUFFER）N＋90，NUMCP \\ CALL BLANK（39，BUFFER） \\ CALL PSSEND（41，BUFFER）
}

690 CONT INUE
700 CONIINUE

TYPE 701
701

＋／／／／／／）
RETURN
END


SUBROUTINE INITPS
DIMENSION ISIAI(1)
LOGICAL*1 BUFFER(BO)
\(\operatorname{ISTAT}(1)=0\)
***** Initialize PS-300 and set up link with PDP-11 using ***** library subroutine. The first two parameters set up ***** logical unit numbers for input from and output to the ***** PS-300. The third parameter indicates whether of not ***** the PS-300 is to issue an "INIT" command. The last ***** two parameters indicate the length and name of the ***** array used to report error status from the PS-300.

TYPE 100
100
FORMATC \({ }^{\prime}\) ***********************************,
\(+\quad /,, \quad * * * * * * * \operatorname{SETIING}\) UP PS-300 *********, \(+\quad /, 1 * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *, ~ / ~ 〕 ~\)
CALL PSETUP(7,7,.IRUE.,1,ISTAT)
CALL PSSEND(11,'INITIALI2E;')

Send file to PS－300 one line at a time，using library subroutine．

OPEN（UNIT＝3，NAME＝＇SPLINE．DAI＇，TYPE＝＇ロLD＇，ERR＝210）
LINE＝ 0
120
\(\operatorname{READ}(3,130, E N D=140, E R R=220)\) ICOUNT，（BUFFER（I）， \(+\quad I=1, I C Q U N T)\)
130 FORMAT（Q，132A1）
IF（ICOUNT．GT．OJCALL PSSEND（ICOUNT，BUFFER）
LINE \(=\) LINE +1
MARK＝LINE－LINE／50＊50
IF（MARK．EQ．O）TYPE 135
135 FORMAT（＇Warking．．．．．＇）
IF（LINE．EQ．1000）TYPE 136
136 FORMAT（＇Don＇＇t give up on me．．．．＇）
GOTD 120
140 CLOSE（3）
REIURN
＊＊＊＊＊Error Routines．
210 TYPE 211
211 FORMATC＇ERROR WHILE OPENING DISK FILE＇， + ＇SPLINE．DAT．＇）

CALL PSEXIT（1，ISTAT） GOTO 140

220 TYPE 2こ1
FORMAT（＇READ ERROR WHILE TRANSFERRING＇，
＇DATA FILE．＇）
CALL PSEXII（1，ISTAT） GOTD 140

END

\section*{Subroutine I口}

SUBRDUTINE ID（KEY）
＊＊＊＊＊This subroutine directs all input／output functions，
＊＊＊＊＊based on the function key press reported in the
＊＊＊＊＊variable＂KEY＂．
REIURN
END


\section*{Subroutine MOUING}

*Input : ICP, IBS,MSG,MCP,NCP, CP(10, 8, 4), vectar fram * *
*Output PS-300 program indicating vertex movement.
*Calls : PSSEND, PSREAD, CPLINE, PSPOLL, BSPLIN
*Alters
: CP(10,8,4)
*Description: This subroutine receives vectars from the *
*
*
*
*
*

*
*
* relocated vertex.
*Created On : 12/17/86 Modified On: *
*
***********************************************************
\begin{tabular}{|c|c|c|}
\hline * Uariable & Iype & Explanation \\
\hline *BUFFER(80) & Logical & Used to pass text messages to and from the PS-300 program. \\
\hline \[
* C P(10,8,4)
\] & Real & The coordinates of the vertices, with* the subscripts indicating row, column, and \(X, Y, Z\) or homogeneous component. \\
\hline * DX & Real & The \(X\) movement of a selected vertex. \\
\hline * DY & Real & The \(Y\) movement of a selected vertex. \\
\hline * 12 & Real & The 2 movement of a selected vertex. \\
\hline * IBS & Integer & Indicates the display status of the \\
\hline & & 1-4=varying combinations of spacing. \\
\hline * ICP & Integer & Indicates the display status of the vertices. ICP=2 indicates the lines connecting the vertices are displayed. \\
\hline * IUEC & Integer & The position of the picked vector in the vector list. \\
\hline *LENGIH & Integer & Byte length of a message returned through a call to PSPOLL or PSREAD. \\
\hline & Integer & The row of vertices under \\
\hline MCP & nteg & The number of rows of vertices \\
\hline
\end{tabular}



SUBROUTINE MQUING (ICP, IBS,MSG, LENGIH, BUFFER)
COMMON /SPLINE/ MCP, NCP, CP(10, 8, 4), MORDER, NORDER LOGICAL*1 BUFFER(BO)

If MSG>100, row or column of vertices has been picked for movement. Compute the appropriate identifying number ( \(81-90=\) raws 1-10; 91-98 = columns 1-8) and send it to the \(P S-300\) program to use in routing the ***** dial signals.
```

    IF (MSG.GT.100) THEN
        IUEC = MSG - 100
        IF (IUEC.LE.MCP*NCP) IHEN
    ```
            a vector in a row of vertices was picked
            NLM \(=(\) IUEC \(+N C P-1) / N C P+B 0\)
            ELSE
                a vector in a column of vertices was picked
                \(N U M=(I U E C+M C P-1-M C P * N C P) / M C P+90\)

ENDIF
ENCDDE (26, 100, BUFFER) NUM
\[
\text { FORMAT ('SEND FIXC', I2,') IO < } 1>\text { PICKED;') }
\]

CALL PSSEND (26, BLFFER) REIURN
ENDIF

A vertex has been maved.
IF (MSG.LT.100) THEN
wait for the vector defining the movement CALL PSREAD (BO, BUFFER,LENGIH)

Decode the message, which is in the form of "L \(X, Y, Z\) ", where \(X, Y\), and \(Z\) are in an E1O Eormat if positive, and an Ell format if negative.

IF (LENGIH.EQ.34) THEN
DECODE ( \(34,200, B \cup F F E R\) ) DX, DY, DZ FORMAT (1X, \(3(1 X, E 10.4)\) )

ELSEIF (LENGTH.EQ.37) THEN
DECODE (37, 201, BUFFER) DX, DY, DZ FORMAT (1X, 3(1X,E11.4))

ELSEIF (LENGTH.EQ.35) THEN
IF (BUFFER(3).EQ.'-') THEN
DECODE (35, 202, BUFFER) DX, DY, DZ FORMAT (2X, E11.4, 2(1X, E10.4))

ELSEIF (BUFFER(14).EQ.'-') THEN
DECODE (35, 203, BUFFER) DX, DY, DZ FORMAT (2X, E10.4,1X,E11.4,1X,E10.4)

ELSE
DECODE ( 35,204, BUFFER) \(D X, D Y, D Z\) FORMAT (1X, 2(1X, E10.4),1X, E11.4)
ENDIF
ELSEIF (LENGTH.EQ.36) IHEN
IF (BUFFER(3).EQ.'-'.AND.BUFFER(15).EQ.'-')
THEN
DECDDE (36, 205, BUFFER) DX, DY, DZ
FORMAI (1X, 2(1X, E11.4),1X,E10.4)
ELSEIF(BUFFER(3).EQ.'-') THEN
DECDDE (36, 206, BUFFER) DX, DY, DZ
FORMAI (2X, E11.4, 1X, E10.4, 1X, E11.4)
ELSE
DECODE ( \(36,207, B \cup F F E R) \quad \mathrm{XX}, \mathrm{DY}, \mathrm{DZ}\)
FORMAT (2X, E10.4, 2(1X,E11.4))
ENDIF

\section*{ELSE}

IYPE 208
208
FORMAT (//,1X, 'UECIOR LENGTH OUT OF RANEE')

RETURN

\section*{ENDIF}

An individual vertex has been moved．
Filter qut accasional erronequs transmissions．
IF（ABS（DX）．GE．0．1）\(\quad D X=0.0\)
IF（ABS（DY）．GE．0．1）\(D Y=0.0\)
IF（ABS（DZ）．GE．0．1）DZ＝0．0
IF（MSG．LE．BO）THEN
\(N=(M S G+9) / 10\)
\(M=M S G-((M S G-1) / 10) * 10\)
\(C P(M, N, 1)=C P(M, N, 1)+D X\) \(C P(M, N, 2)=C P(M, N, 2)+D Y\) \(C P(M, N, 3)=C P(M, N, 3)+D Z\)
ENDIF
A row or column of vertices has been moved．
IF（MSG．GI．BO）THEN
IF（MSG．LE．SO）THEN
a row has been moved \(M=\) MSG－BO ロロ 210 \(N=1\) ，NCP
\(C P(M, N, 1)=C P(M, N, 1)+\square X\)
\(C P(M, N, 2)=C P(M, N, 2)+\square Y\) \(C P(M, N, 3)=C P(M, N, 3)+D Z\)
CONI INUE
ENDIF
IF（MSG．GI．90）THEN
a column has been moved \(N=\) MSG－ 90
ロO 220 M＝1，MCP
\(C P(M, N, 1)=\operatorname{CP}(M, N, 1)+\square X\)
\(C P(M, N, 2)=C P(M, N, 2)+D Y\)
\(C P(M, N, 3)=C P(M, N, 3)+D 2\)
220
CONIINUE
ENDIF
ENDIF
Report the new B－spline surface and vertices＇ vectars to the \(P S-300\) anly if vertex movement is completed，to minimize transmission time．

\author{
IF (IBS.ET.O) CALL BSPLIN ENDIF
}

RETURN
ENDIF
SIDP
END

\section*{SUBROUTINE PLANES(IPLANE)}
***** When implemented, this subroutine will calulate and ***** transmit to the PS-300 the intersection of the
***** B-spline surface with the orthogonal plane specified ***** by IPLANE.

RETURN
END


＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊SUBRDUTINE PREPS
\(\square\)
＊
＊Input ：PREPS－Earmat data file defining＊
＊
＊ロutput ＊
＊Calls
＊Alters
＊Description：This subroutine reads a data file of points
＊Created By ：D．Michael Bryant
＊Created \(0 n\) ： \(4 / 20 / 87\) Madified \(0 n\) ：

\[
*
\]
Explanatian＊

＊BUFFER（BO）Logical ＊
＊FILNAM Char
＊
＊
＊ICOORD Intege
＊IGNORE
＊
＊
＊IOSTAI
Integer
Integer
＊IREF
＊
＊
＊ISIAR

Contains strings being received from＊ or sent to the PS－300．
Name of the PREPS－farmat data file＊ containing the data for the known＊ paints．＊
Coordinate to be held constant for＊ each repetition of the substructure＊ directed by NPTS2．\(O=\) nane； \(1=X ; 2=Y\) ； \(\exists=2\) 。
Dummy variable used to read data from＊ PREPS－Farmat Eile which is not needed＊ by this program．
Reparts input／autput errar status．＊ Plane about which substructure is to＊ be reflected． \(0=\) nane； \(1=Y Z\) ；＊乙 \(=X Z ; \quad \exists=X Y\) ．
Number of vector components required to define the position of stars used＊ to represent data points from data＊ file on the PS－300 screen．A＊ maximum of 199 points can be sa＊ labeled，although the structure can＊

\begin{tabular}{|c|c|c|}
\hline & Integer & \begin{tabular}{l}
contain many more points. \\
Identifies the element of UECS which contains the 2 vector component of the final vector in the previausly processed substructure.
\end{tabular} \\
\hline *LP(1000 & Logical & Contains "paint" (.FALSE.) or "line" (.TRUE.) designations for the itemized vector list defined by UECS. \\
\hline *MAXUE & Intege & Number of vector components which the current substructure adds to UECS. \\
\hline & Integ & Value greater than zera indicates end of data file has been reached. \\
\hline *N & Intege & Number of paints defining the current substructura. \\
\hline & Int & Number of repetitions of the substructure to be constructed. \\
\hline *NSTRUC & Intege & Number identifying the current partion of the known data being processed. Ia minimize memory consumption, the known data is split into a number of vector lists rather than a single lang ane. \\
\hline *REPEAT(10) & Real & Contains the values of the coordinat specified by ICODRD to be used with repetitions af a substructure. \\
\hline *UECS(3000) & Real & Contains the vectors for the vector list to be transmitted to the PS-300. \\
\hline * XBODY & Real & Glabal translation along the \(X\) axis to be applied to the structure. Applied befare narmalization. \\
\hline * XNORM & Real & Normalization factor by which all vectors in data file are to be divided. \\
\hline & Real & Iranslation of substructure along \(X\) axis. Applied before normalizatio \\
\hline & Real & Global translation along the \(Y\) axis to be applied to the structure. Applied befare normalization. \\
\hline & Real & Iranslation of substructure along t Y axis. Applied before normalizatio \\
\hline *ZBODY & Real & Global translation along the \(Z\) axis to be applied to the structure. Applied before normalization. \\
\hline * ZIRAN & Real & Translation of substructure along th 2 axis. Applied before normalization \\
\hline
\end{tabular}

SUBROUTINE PREPS
COMMDN /UECS/ UECS(1000)
DIMENSION REPEAT(10)
LロGICAL LP(33ヨ)


LOGICAL*1 BUFFER(BO)
CHARACTER*日O FILNAM
NSTRUC = 1
NDONE \(=0\)
IUEC = 0
TYPE *, ' ENTER FILE NAME.'
READ (5,5) FILNAM
5
FORMAT (ABO)
OPEN (UNIT=3, NAME=FILNAM, TYPE='OLD',ERR=2OO)
Read global header.
READ ( \(3, *, E R R=300)\) XNORM
READ (3,*, ERR=300) IGNDRE
READ ( \(3, *, E R R=300)\) XBODY, YBODY, ZBDDY
Read substructure header and data.
10 READ ( \(3, *, E N D=500, E R R=300\) ) NPIS, NPIS2, ICOORD
READ ( \(3, *, E R R=300\) ) XTRAN, YTRAN, ZTRAN, IREF
Ensure the UECS array dimension will not be exceeded by reading the substructure data.
```

MAXUEC = NPTS*NPTS2*3
IF (IREF.NE.O) MAXUEC = MAXUEC*2
IF (IUEC+MAXUEC.GT.100O) THEN
GOTD 400
ENDIF

```

Read substructure data.
15 CDNTINUE
IF (ICOARD.NE.1) THEN
READ ( \(3, *, E R R=300\) ) (UECS (IUEC+ \(I * 3-2), I=1\),NPTS) ELSE
\(\operatorname{READ}(3, *, E R R=300)(R E P E A T(I), I=1\), NPTS2)
ENDIF
IF (ICOORD.NE.2) THEN
\(\operatorname{READ}(3, *, E R R=300)(U E C S(I U E C+I * 3-1), I=1\),NPTS)
ELSE
\(\operatorname{READ}(3, *, E R R=300)(R E P E A T(I), I=1\),NPIS2)
ENDIF
IF (ICDORD.NE. 3) THEN
READ ( \(3, *, E R R=300\) ) (UECS(IUEC+I*3), \(I=1\), NPTS)
ELSE
\(\operatorname{READ}(3, *, E R R=300)(R E P E A T(I), I=1, N P T S 2)\)

ENDIF
IYPE *, ' Warking
Construct substructure repetitions and perform translations and normalization.

DO \(30 \mathrm{I}=1\),NPIS2
\(20 \mathrm{~J}=1\), NPTS
\(\mathrm{L}=(\mathrm{I}-1) *\) NPIS*3
IF (ICOORD.EQ.1) THEN UECS (IUEC+J*ヨ-2+1) = (REPEAT (I) +XIRAN+XBCDY)/XNDRM-0.5
ELSE
\(\operatorname{UECS}(\operatorname{IUEC}+J * 3-2+1)=\)
\(+\quad(\) UECS (IUEC \(+J * 3-2)+X I R A N+X B C D Y) /\)
+ XNORM-0.5
ENDIF
IF (ICOORD.EQ.2) THEN UECS (IUEC+J*3-1+1) = (REPEAI (I) + YIRAN+YBODY)/XNORM
ELSE
UECS (IUEC+J*3-1+L) =
(UECS (IUEC+J*3-1) +YIRAN+YBODY)/XNORM
ENDIF
IF (ICOQRD.ED.3) THEN
UECS (IUEC \(+J * 3+L\) ) \(=\)
(REPEAI (I) + ZIRAN+ZBODY)/XNQRM
ELSE
UECS (IUEC \(+J * 3+L\) ) =
(UECS (IUEC+J*3) + ZIRAN + ZBODY) / XNORM
ENDIF
\(\operatorname{LP}((I-1) * N P I S+J+I U E C / 3)=\). IRUE. IF(J.EQ.1) LP((I-1)*NPIS+J+IUEC/3)=.FALSE.

CONT INUE
CONI INUE
Construct substructure reflections.
```

IF (IREF.GT.O) THEN
DO 40 I = IUEC, IUEC+MAXUEC/2-3,3
00 35 J = 1,3
UECS(I +J +MAXUEC/2)=UECS(I +J )
CDNTINUE
UECS(I + IREF+MAXUEC/2) = UECS(I + IREF)*(-1.0)
LP((I +MAXUEC/2)/3+1)=LP(I/3+1)

```


ENDIF
```

IUEC = IUEC + MAXUEC
GOTD 10

```
Errar statements.


Define the position of stars to represent up to 199 data points.

400 IF (NSIRUC.EQ.1) THEN ISTAR = 199*3
IF (IUEC.LI.ISIAR) ISTAR = IUEC
DO 450 I \(=3\), ISTAR, 3
IF (I-I/10*10.EQ.O) IYPE *,' warking.... ENCDDE ( \(61,410, B \cup F F E R) I / 3, \operatorname{UECS}(I-2)\), UECS (I-1), UECS (I)
410

450 CONTINUE
ENDIF
Send vector list for partial structure to PS-300.
ENCODE ( \(33,460, B \cup F F E R\) ) NSTRUC, IUEC/3
460
FORMAT ('KL', I2,':=UECTOR_LIST IIEMIZED \(\mathrm{N}=\) =', I 4)
CALL BLANK ( \(3, B \cup F F E R\) )
CALL PSSEND (33, BUFFER)
CALL PSUECS (4, IUEC/3, UECS,LP,. TRUE., IDSIAT)
```

NSTRUC = NSTRUC + 1
IUEC = O
IF (NDONE.EQ.1) GOTD 600
GOID }1

```


********************************************************** ********************************************************** ******************** Subrautine REFLCI *****************
 ********************************************************

\section*{SUBROUTINE REFLCI}
***** This subroutine will calculate and display a
***** reflection of the displayed B-spline surface about
***** the body's XZ plane.



RETURN




\section*{SUBRQUIINE RESET(IRESET)}

\section*{LOGICAL*1 BUFFER(BO)}

CALL PSSEND (31,'SEND U(0,0,0) TD <2>IRAN IOIAL;')
CALL PSSEND(29,'SEND U(O,0,0) ID <1>ALL.IRAN;')
CALL PSSEND(19,'SEND 1 TD <2>SCALE;')
CALL PSSEND(19,'SEND O TD <1>SCALE;')
IF (IRESEI.GI.1) THEN
CALL PSSEND(22, 'SEND 90 ID <1>RESEI X;') ELSE

CALL PSSEND(21,'SEND 0 TD <1>RESEI_X;') ENDIF

IF (IRESET.EQ.3) THEN
CALL PSSEND(22,'SEND 90 ID <1>RESEI_Y;')
ELSE
CALL PSSEND(21,'SEND O ID < 1>RESEI Y;')
ENDIF
REIURN
END



SUBROUTINE SURFAC
Lagical Lp(333)
COMMDN /UECS/ UECS(1000)
COMMON /BASIS/ R(13,4,31), \(S(11,4,31), \operatorname{SURF}(3,31,31)\) LOGICAL*1 BUFFER(BO)

NSTRUC = 0
Parametric lines in u (longitudinal) direction.
10 CONTINUE
NSTRUC = NSTRUC + 1
\(\mathrm{NU}=310\)
IUECS \(=0\)
ILP \(=0\)
NBEGIN \(=(N S T R U C-1) * 10+1\)
NEND = NSTRUC*10
IF (NSTRUC.EQ.4) THEN
NEND = NBEGIN
\(\mathrm{NU}=31\)
ENDIF
DO 100 I = NBEGIN,NEND
DO \(90 \mathrm{~J}=1,31\)
Count the vectors created.
ILP = ILP + 1
DO \(80 \mathrm{~K}=1,3\)
Count the vector components (x,y,z). IUECS = IUECS + 1 UECS(IUECS) \(=\operatorname{SURF}(K, I, J)\)
CONTINUE
Indicate whether vector is point or line vector.
LP(ILP) = .TRUE.
IF (J.EQ.1) LP(ILP) = .FALSE.
CONTINUE
90
100 CONTINUE
GOTO 300
Parametric lines in w (transverse) direction.
110 CONTINUE
NSTRUC = NSTRUC + 1
\(\mathrm{NU}=310\)
IUECS = 0
ILP \(=0\)
NBEGIN \(=(N S T R U C-5) * 10+1\)
NEND = (NSTRUC-4)*10

\begin{tabular}{|c|c|}
\hline & \begin{tabular}{l}
IF (NSTRUC.EQ.Q) THEN \\
NEND \(=\) NBEGIN \\
\(N U=31\)
\end{tabular} \\
\hline \multicolumn{2}{|r|}{ENDIF} \\
\hline \multicolumn{2}{|r|}{DO 2OO J = NBEGIN, NEND} \\
\hline & DO \(190 \mathrm{I}=1,31\) \\
\hline & \begin{tabular}{l}
ILP \(=I L P+1\) \\
प0 \(180 \mathrm{~K}=1,3\)
\end{tabular} \\
\hline & IUECS \(=\) IUECS +1 \\
\hline \multicolumn{2}{|r|}{UECS (IUECS \(=\) SURF (K, I , J )} \\
\hline \multicolumn{2}{|l|}{180 CONIINUE} \\
\hline \multicolumn{2}{|r|}{\(L P(I L P)=\). TRUE.} \\
\hline \multicolumn{2}{|r|}{\(I F(I . E Q .1) L P(I L P)=. F A L S E\).} \\
\hline \multicolumn{2}{|l|}{190 CONIINUE} \\
\hline 200 & CONTINUE \\
\hline \multirow[t]{2}{*}{300} & CONIINUE \\
\hline & ENCODE ( \(31,310, B \cup F F E R\) ) NSTRUC, NU \\
\hline \multirow[t]{8}{*}{310} & FORMAT ('BS', I 1 , \({ }^{\prime}=\) UECIOR LISI ITEMIZED \(N=\), I 3 ) \\
\hline & CALL PSSEND ( \(31, B \cup F F E R\) ) \\
\hline & CALL PSUECS ( \(4, I L P\), UECS, LP, TRUE., IOSIAT) \\
\hline & TYPE *, Warking.... \\
\hline & IF (NSTRUC.LI.4) GOTD 10 \\
\hline & IF (NSTRUC.LI.8) GOID 110 \\
\hline & RETURN \\
\hline & END \\
\hline
\end{tabular}

Subroutine WaIT
* IXY, IXZ,IYZ, and PS-300 equivalents *
*Calls : BSPLIN,CPLINE,ID,MOUING,PLANES,PSREAD, *
* PSSEND,REFLCI,RESEI *
*Alters : *
*Description: Awaits signals under the contral of the *

*BUFFER(BO)
*
*IBS Integer
*
*ICLIP
* ICP
*
* I KNUWN
*
*
*IPICK
*
*
* IRESEI
*
*IRFLCI
*
*
*IXY
*
*
*
* IXZ
* IYZ
*LENGIH
*
*MODE Integer

Type Explanation

Logical

Integer
Integer

Integer

Integer

Integer
Integer

INTEGER

Integer
Integer
Integer

Integer See IXY. See IXY. PS-300, in bytes.

Contains strings being received from or sent to the PS-300.
Status of B-spline surface display: * \(0=\) not displayed, \(1=\) displayed. * 2-clipping status: 1=off, \(2=0 n\). * Contral polygon display status: \(0=\) not* displayed, \(1=p o i n t s ~ d i s p l a y e d, ~ *\) 2=connecting lines displayed. * Display status of known surface: * O=not displayed, \(1=\) points displayed, * \(2=c o n n e c t i n g\) lines displayed.
Picking mode indicator: \(1=\) micking * individual vertices, \(2=p i c k i n g\) rows * or columns of vertices.
Reset toggle indicator: \(1=(X 0, Y O, 20)\),* \(2=(X 90, Y 0,20), \quad 3=(X 90, Y 90,20)\). Status of display of reflection of * B-spline surface about an X2 plane: * O=not displayed, \(1=d i s p l a y e d\). Status of display of intersection of * B-spline surface with XY orthogonal * plane (waterlines): \(0=\) not displayed, * \(1=\) coarse spacing, 2=fine spacing. * Length of incoming message from *

Function key availability status: *
\(1=\) standard mode, most functions * available, \(2=d i s p l a y\) of reflection or* intersection with planes selected, * interactive mode not available, \(3=i n t e r a c t i v e ~ m o d e ~ s e l e c t e d\), \(4=i n p u t / o u t p u t\) menu selected.
Contains a numeric message Erom the * PS-300, as decoded from BUFFER. \(1-80\) indicate next message will be a * new vector for the vertex of the same* number. 101-242 indicate next
message will be new vector of the * vertex in the row or column of the * contral polygon line which has the * position in the vector list ( \(N-100\) ). * 301-312 indicate a keypress of function keys 1-12.


SUBRDUIINE WAIT

LOGICAL*1 BUFFER(8O)
```

Initialize variables for default operating modes.
LENGIH = 0
MODE=1
ICP=1
I BS=0
IKNDWN=0
IPICK=1
ICLIP=1
IRFLCI=0
I XY=0
IXZ=0
IYZ=0
IRESET=3
***** Receive and decode integer message from PS-300
***** program.
100 IF (LENGIH.GI.O) GDID 190

* LENGIH > 0 indicates message already received in another subroutine.
110 CALL PSPOLL(BO,BUFFER,LENGTH)
IF (LENGIH.EQ.O) GDTD 110
190 DECDDE(LENGTH,2OO, BUFFER) MSG
200 FORMAT (I3)
LENGTH $=0$
If message indicates new vertex vector is coming, go to subrautine MOUING to receive and act upon the vector.
IF (MODE.EQ.3.AND.MSG.LT.300) THEN
CALL MDUING (ICP, IBS,MSG, LENGTH, BUFFER)
ENDIF
IF (MODE.EQ.3.AND.MSG.LT.300) GOTD 100
Uertex display toggle.
IF (MODE.LE.3) THEN
IF (MSG.EQ.301) THEN
$I C P=I C P+1$
IF (ICP.GI.2) ICP=0
IF (ICP.EQ.2) CALL CPLINE ENCODE (25, 300, BUFFER) ICP CALL PSSEND (25, BUFFER)


B-spline surface display toggle.
IF (MSG.EQ.302) THEN
IBS=IBS+1
IF (IBS.GT.1) IBS=0
IF (IBS.GT.O) CALL BSPLIN
ENCODE (25, 310, BUFFER) IBS
FORMAT ('SEND FIXC'I1') TO <1>BSMODE;')
CALL PSSEND (25, BUFFER)
ENDIF
Known surface display toggle.
IF (MSG.EQ.303) THEN
I KNDWN=IKNOWN+1
IF (IKNOWN.GT.2) IKNOWN=0
ENCODE (28, 320, BUFFER) IKNDWN
320 FORMAT('SEND FIXC'I1') TO <1>KNDWNMODE;') CALL PSSEND (28,BUFFER)
ENDIF
Interactive mode toggle.
IF (MSG.EQ.304) THEN
IF (MODE.EQ.1) THEN MODE=3
ELSEIF CMODE.EQ.3) THEN MODE $=1$
ENDIF
ENCODE (23,330,BUFFER) MODE
330
FORMAT ('SEND FIXC'I1') TD <1>MODE;')
CALL PSSEND (23,BLFFER)
ENDIF
Z-clipping toggle.
IF (MSG.EQ.305) THEN
ICLIP=ICLIP+1
IF (ICLIP.GT.2) ICLIP=1
ENCODE (27, 340, BUFFER) ICLIP
340 FORMAT ('SEND FIXC'I1') TO <1>CLIPMODE;')
CALL PSSEND (27, BUFFER)
ENDIF
Reflection display toggle.
C
C
C
C
IF (MSG.EQ.305) THEN
IF (MODE.EQ.1) THEN MODE=2
I RFLCT=1




```
C
C
C
**** Row-to-point pi
Row-to-point picking toggle.
    IF (MODE.EQ.3.AND.IPICK.EQ.Z) THEN
    I P ICK=1
    CALL PSSEND (27,
                                    'SEND FIX(1) TO <1>PICKMODE;')
    ENDIF
        ENDIF
```

    YZ intersection display toggle.
    | C | IF (MSG.EQ.309.AND.MODE.LT.3) THEN |
| :---: | :---: |
| C | $I Y Z=I Y Z+1$ |
| C | IF (IYZ.GT.2) IYZ=0 |
| C | IF (IYZ.EQ.1) CALL PLANES(3) |
| C | ENCODE (25, 380, BUFFER) IYZ |
| C380 | FORMAI ('SEND FIX ${ }^{\text {('I1') }}$ IO <1>YZMODE;') |
| C | CALL PSSEND (25, BUFFER) |
| C | IF (IYZ.EQ.O) GOID 400 |
| C | ENDIF |

Select input/output menu.
IF (MSG.EQ.310) IHEN
LAST = MODE
MODE $=4$
CALL PSSEND (23,'SEND FIX(4) ID <1>MODE;')
ENDIF
Reset function toggle.
IF (MSG.EQ. 311) THEN
IRESET = IRESET +1
IF (IRESET.GT.3) IRESET=1
CALL RESET (IRESET)
ENDIF

Quit.
IF (MSG.EQ.312) THEN
CALL PSSEND (11,'INITIALIZE;')
RETURN
ENDIF
ENDIF
I/0 menu selections.
IF (MODE.EQ.4) THEN
IF (MSG.LT.312) CALL IO(MSG-300)


```
        IF (MSG.EQ.312) IHEN
                MODE = LAST
                ENCODE (23, 330,BUFFER) MODE
                CALL PSSEND (23,BUFFER)
            ENDIF
```

    ENDIF
    Irigger PS-300 program to send new variable values to
    all 'FETCH' nodes.
    CALL PSSEND (2己, SEND 1 ID < 1>NEW_MODE;')
    GOID 100
    If toggling a function 'off' while in mode 2 , ensure
    all mode-2 functions are off before returning to
    mode 1.
    400 IFCIRFLCT.EQ.O.AND.IXY.EQ.O.AND.IXZ.EQ.O.AND.IYZ.EQ.O
+ ) THEN
MODE = 1
CALL PSSEND (23,'SEND FIX(1) ID <1>MODE;')
CALL PSSEND (ट己, 'SEND 1 TD <1>NEW_MDDE;')
ENDIF
GOID 100

END

APPENDIX C
SPLINE.DAT PROGRAM LISTING

SPLINE.DAT is the PS 300-resident portion of the program, SPLINE.

I . Variables.
II. Main display tree.
A. Display vertices.
B. Display B-spline surface.
C. Display points on known surface.
D. Display reflection of all displayed structures about a plane.
E. Display intersection of XY planes with B-spline surface.
F. Display intersection of $X Z$ planes with B-spline surface.
G. Display intersection of $Y Z$ planes with B-spline surface.
III. Connect dials.
A. Iranslation.
B. Rotation.
C. Scaling.

IU. Uertex picking netwark.
A. Enable picking.
B. Convert cursar position to picklist.
C. Canvert picklist to integer identifying vertex.
D. Report pick of row or column to host computer.
E. Route translation dial signals ta picked vertices
U. Repart vertex mavement to host.

UI. Clipping.
UII. Function keys and labels.
A. Report key press to host computer.
B. Label function keys and dials.


3
SEND
＇SPLINE，A B－SPLINE SURFACE MODELER BY D．MICHAEL BRYANT＇


## \｛\}

TD＿HOST：$=$ F：PRINT；\｛Convert messages going to host to strings？
CONNECT TO＿HOST＜1＞：＜1＞HOST＿MESSAGE； SEND IRUE TO 〈ट〉IO HOSI；
\｛\}
NEW＿MODE：$=F: N O P$ ；

## \｛\}

UARIABLE BSMODE；

SEND FIX（1）TO＜ $1>B S M O D E$ ； FEICHBSMDDE：$=$ F：FETCH；

SEND＇BSMODE＇TO＜ᄅ＞FETCHBSMODE；
CONNECI NEW＿MODE＜1＞：＜1＞FETCHBSMODE；

## \｛\}

UARIABLE CLIPMODE；
\｛Z－clipping mode： $1=o f f$, 2＝0n\}
SEND FIX（1）TO＜1＞CLIPMODE；\｛Initial default value\} FEICHCLIPMODE：＝F：FEICH；

SEND＇CLIPMODE＇ID＜ C •FEICHCLIPMDDE；
CONNECT NEW＿MODE＜1＞：＜1＞FEICHCLIPMODE；

## \｛\}

UARIABLE CPMODE；
〔Control point display mode： $0=n o t$ displayed， 1＝points displayed， ᄅ＝connecting lines\} \｛Initial default value\} SEND FIX（2）IO＜1＞CPMDDE； FEICHCPMDDE：$=\mathrm{F}:$ FEICH；

SEND＇CPMODE＇ID＜ᄅ＞FETCHCPMODE；
CONNECT NEW MODE＜1＞：＜1＞FETCHCPMODE；
\｛\}

UARIABLE DISCARD;

## \{\}

UARIABLE KNOWNMODE;

SEND FIX(O) TO <1>KNDUNMODE; \{Initial default value\}
\{Provides connection for function outputs left intentionally unused, without receiving a "no connection made to ...." error message on screen\}

〔Known surface display mode: $0=n o t$ displayed, 1=points displayed, 2=connecting lines\} FETCHKNDUNMODE: $=F: F E T C H$;

SEND 'KNOWNMODE' IO <2>FETCHKNOWNMODE;
CONNECT NEW_MODE<1>:<1>FETCHKNOWNMODE;

## [\}

UARIABLE MODE;

SEND FIXC1) TO <1>MODE;
FETCHMODE: =F:FETCH;
SEND 'MODE' TO <2>FETCHMODE;
CONNECT NEW_MODE<1>:<1>FETCHMODE;

## \{\}

UARIABLE PICKMODE;

> SEND FIX(1) TO <1>PICKMODE;

〔Uertex picking mode:
l=individual points,
2=rows/columns of
pointss
\{Initial default value\} FETCHPICKMODE: =F:FETCH;

SEND 'PICKMODE' IO <2>FETCHPICKMODE;
CONNECT NEW_MODE<1>:<1>FETCHPICKMODE;

## \{\}

UARIABLE REFLECTMODE; \{Reflection-about-plane display status: 0=off, 1=0n\}
SEND FIX (O) TO <1>REFLECTMODE; \{Initial default value\} FETCHREFLECTMODE: =F:FETCH;

SEND 'REFLECTMODE' TO <2>FETCHREFLECTMODE;
CONNECT NEW MODE<1>:<1>FETCHREFLECTMODE;
\{\}

UARIABLE XYMODE，XZMODE，YZMODE；

SEND FIX（O）TD＜ 1 ＞XYMODE； FEICHXYMDDE：$=$ F：FETCH；

SEND＇XYMODE＇TO＜ $2>F E I C H X Y M O D E ;$
CONNECI NEW MODE＜1＞：＜1＞FEICHXYMODE； SEND FIX（O）IO＜ $1>$ XZMODE；$\{I n i t i a l ~ d e f a u l t ~ v a l u e\} ~$ FETCHXZMODE：$=\mathrm{F}:$ FEICH；

SEND＇XZMODE＇IO＜ट＞FETCHXZMODE；
CONNECT NEW＿MODE＜1＞：＜1＞FETCHXZMODE；
SEND FIX（O）IO＜1＞YZMODE；\｛Initial default value\} FETCHYZMODE：＝F：FETCH；

SEND＇YZMODE＇IO＜ट＞FEICHYZMODE；
CONNECI NEW＿MODE＜1＞：＜1＞FETCHYZMODE；
〔

3
CLIPON：＝SEI DEPTH CLIPPING $\square F F$ APPLIED ID CLIPPER；
CLIPPER：$=$ WINDOW $X=-1: 1 \quad Y=-1: 1 \quad$ FRONT $=0$
BACK＝0．1 APPLIED ID CLIP＿INTENSIIY；
CLIP＿INTENSITY：＝SET INTENSITY OFF 1：1 APPLIED TO ALL；〔Disables depth cueing when clipping is on，to allow viewing within narrow clipping windows\}
DISPLAY CLIPON；
ALL：＝BEGIN SIRUCIURE
UIEWPORT HOR＝－1：1 UERT＝－1：1 INTENSITY＝．75：1；
TRAN：＝TRANSLATE BY $0,0,0$ ；
ROT：＝ROTATE O；
SCALE：＝SCALE BY 1；
SEI：＝SET CONDIIIONAL BII 1 ON；
INSTANCE $\square F$ CP SET，BS SET，KNOWN SET，PLANE SEI； END STRUCIURE；
CP_SET: = SET LEUEL_ロF_DETAIL TD 1 THEN CP_IF;
\{Node to connect toggle
to\}

CDNNECT FETEHCPMODE《1》：《1＞CP＿SET；
CP＿IF：＝IF LEUEL＿OF＿DETAIL＞O THEN CP；
\｛Display vertices unless toggled off．\}
CP：＝INSTANCE OF CP＿PT，CP＿LINES；\｛Structure consists of two branches：points and connecting lines．\}
CP＿LINES：＝BEGIN＿STRUCTURE
IF LEUEL＿OF＿DETAIL＝2； \｛Display if toggled on．\} SETPICK：＝SET PICKING DFF；
\｛Create picking node to allow vertices to be moved a row or column at a time by picking the connecting line\}
SEI PICKING IDENTIFIER＝CPG9；
INSTANCE OF CPL；$\quad$ CCPL is a vector list which will be provided dynamically by the host computer． 3
CPL：＝UECTOR LIST ITEMIZED N＝200
0．0，0．0，0．0；\｛Reserve memory for vector list．\}
END＿STRUCTURE；
［\}
CP PI：＝BEGIN STRUCTURE
SETPICK：$=$ SET PICKING $O F F ;$ CCreate picking node to allow vertices to be selected in interactive made by picking with tablet and stylus？
INSTANCE OF
CPO1，СРO2，С． CPO9，CP10，CP11，CP12，CP13，CP14，CP15，CP16， CP17，CP1日，CP19，CP20，CP21，CP22，CP23，CP24，

 СР41，СР42，СР4 З，СР44，СР45，СР46，СР47，СР4日， CP49，СP50，CPS1，CPS2，CP53，CP54，CP55，CP56， CP57，CP5日，CP59，CP60，CP61，CP62，CP63，СP64， CP65，CP66，CP67，CP6日，CP69，CP70，CP71，CP72， СР73，СР74，СР75，СР76，СР77，СР7日，СР79，СР8О； END＿STRUCTURE；

〔
Definitions of CPOl through CP80 will be supplied by the host computer, with the necessary nodes and connections to allow the vertices ta be individually manipulated in the interactive mode. The pragram lines supplied dynamically from the host computer will have the following form (with the 01 replaced with the appropriate number far the nodes associated with each vertex):
*CPO1:=BEGIN_STRUCTURE

* SET PICKING IDENTIFIER=CPO1
* TRAN: = IRANSLATE BY 0,0,0
* INSTANCE DF CUBE
* END_STRUCTURE
* 

*TRAN_TOTAL 01: =F: ACCUMULATE
(Create translation accumulator far each vertex. $)$

* CDNNECT TRAN_IDTAL_01<1>:<1>CPO1.IRAN

SEND $U(X, Y, Z)$ ID < $2>$ IRAN_IDIAL_O1
(Initial vertex position.)
SEND $U(0,0,0)$ TO <1>TRAN_TDTAL_O1
(Give accumulator an initial value to act upan befare input Erom dial is received).
SEND 0.1 TD < $4>$ TRAN_TOTAL 01 (Multiplier for dial sensitivity.)

CUBE: = INSTANCE DF FRDNT, BACK,SIDES; \{Each vertex is
represented on the
screen by a cube. $\}$
BACK: =TRANSLATE BY 0,0,0.01 APPLIED ID FRONT; FRDNT:=UECTDR LIST $Z=-0.005 \mathrm{~N}=5$

$$
\begin{array}{rrr}
-0.005,-0.005 & 0.005,-0.005 & 0.005,0.005 \\
-0.005, & 0.005 & -0.005,-0.005 ;
\end{array}
$$

SIDES：＝UECIDR LIST SEP $N=\theta$

| -0.005, | $0.005,0.005$ | $-0.005,0.005,-0.005$ |
| ---: | ---: | ---: |
| $-0.005,-0.005,0.005$ | $-0.005,-0.005,-0.005$ |  |
| $0.005,0.005,0.005$ | $0.005,0.005,-0.005$ |  |
| $0.005,-0.005,0.005$ | $0.005,-0.005,-0.005 ;$ |  |

〔
＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊Display B－Spline Surface＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊
\}
BS＿SET：＝SET LEUEL＿OF＿＿ETAIL TD 1 THEN BS＿IF；
\｛Display B－spline
surface if toggled on．\}
CONNECT FETCHBSMODE＜1＞：＜1＞BS＿SET；
BS＿IF：＝IF LEUEL＿OF＿DETAIL＞O THEN BS；
BS：＝INSTANCE $\square F$ BS1，BS2，BS3，BS4，BS5，BS5，BS7，BS9；
〔
The host computer will dynamically provide program lines defining $B S$ ．These commands will be of the form：

```
* BS1:=UECTOR_LISI ITEMIZED N=XXX *
```

3
〔
************* Display Paints on Known Surface ************
3

KNDWN SET：＝SET LEUEL OF DETAIL TD 1 THEN KNDWN IF； \｛Display known points if toggled on． 3
CONNECT FETCHKNOWNMODE＜1＞：＜1＞KNOUN＿SET；
KNOUN＿IF：＝IF LEUEL＿OF＿DETAIL＞O IHEN KNOWN； KNOWN：＝INSTANCE OF KNDUN＿PIS，KNOUN＿LINES；

## \｛\}

KNOUN PTS：＝INSTANCE DF
KPTOO1，KPTOO2，KPTOO3，KPTOO4，KPTOO5，KPTOOE， KPTOO7，KPTOOQ，KPTOO9，KPT010，KPTO11，KPIO1己， KPT013，KPTO14，KPTO15，KPT016，KPTO17，KPTO1日， KPTO19，KPTO20，KPTO21，KPTO2ᄅ，KPTO23，KPTO24， KPIO25，KPTO26，KPTO27，KPTO29，KPTO29，KPTO29， KPIO30，KPTO31，KPTO32，KPTO33，KPIO34，KPIO35， KPT036，KPT037，KPTO38，KPTO39，KPTO40，KPTO41， KPIO42，KPIO43，KPTO44，KPTO45，KPTO46，KPIO47， KPIO49，KPIO49，KPIOSO，KPTOS1，KPTOS2，KPIOS3， KPTO54，KPTO55，KPTOS6，KPT057，KPIOS日，KPTO59， KPTOEO，KPTOE1，KPIOEこ，KPIOE3，KPTOE4，KPTOG5， KPIO65，KPIO67，KPTO68，KPIO69，KPTO70，KPT071， KPIO72，KPIO73，KPTO74，KPTO75，KPIO75，KPIO77， KPIO7日，KPIO79，KPTO80，KPTO日1，KPIO82，KPIO83， KPTO日4，KPIO85，KPTO86，KPTO87，KPTO日日，KPIO日9，


```
KPTO90, KPTO91, KPTO92, KPTO93, KPTO94, KPTO95,
KPTO9G, KPTO97, KPTO9日, KPTO99, KPT100, KPT101,
KPT102, KPT103, KPT104, KPT105, KPT105, KPT107,
KPT10日, KPT109, KPT110, KPT111, KPT112, KPT113,
KPT114, KPT115, KPT115, KPT117, KPT11日, KPT119,
KPT120, KPI121, KPT122, KPI123, KPI124, KPT125,
KPT126, KPT127, KPT128, KPT129, KPT130, KPT131,
KPT132, KPT133, KPT134, KPT135, KPT136, KPT137,
KPT139, KPT139, KPI140, KPT141, KPT142, KPT143,
KPT144, KPT145, KPT146, KPT147, KPT148, KPT149,
KPT150, KPT151, KPT152, KPT153, KPT154, KPT155,
KPT156, KPT157, KPT15日, KPT159, KPT160, KPT161,
KPT162, KPT153, KPT154, KPT155, KPT155, KPT157,
KPT168, KPT169, KPT170, KPT171, KPT172, KPT173,
KPT174, KPT175, KPT175, KPT177, KPT178, KPT179,
KPT180, KPT181, KPT182, KPT183, KPT184, KPT185,
KPT185, KPT187, KPT188, KPT189, KPT190, KPT191,
KPT192, KPI193, KPI194, KPI195, KPI196, KPI197,
KPI198, KPI199;
{
```

Structures KPTOO1 through KPT199 will be provided dynamically by the host computer．The commands provided will be of the form：
＊KPTO37：＝TRANSLATE BY $x, y, z$ APPLIED TO STAR
3
STAR：＝UECTOR LIST SEP N＝14

| 0.000, | 0.005, | 0.000 | $0.000,-0.005$, |
| ---: | ---: | ---: | ---: | 0.000

## \｛ $\}$

KNOWN＿LINES：＝IF LEUEL＿OF＿DETAIL＝2 THEN KLINES； CDisplay lines connecting known points if toggled on． 3
KLINES：＝INSTANCE OF KLO1，KLO2，KLO3，KLO4，KLO5，KLOE，KLO7， KLO日，KLO9，KL10，KL11，KL12，KL13，KL14；

## 〔

KLINES，the vector list defining the lines connecting the known points，will be provided dynamically by the host computer．The command provided by the host will be of the farm：

$$
\text { KLO1: =UECTOR_LIST ITEMIZED } N=x \times x
$$


＊＊＊＊＊＊＊＊＊＊＊＊Display Reflection About a Plane＊＊＊＊＊＊＊＊＊＊＊＊
3
REFLECT SET：＝SET LEUEL＿DF DETAIL TD O THEN REFLECT＿IF；
\｛Display reflection
if toggled on．\}
CDNNECI FETCHREFLECTMDDE＜1＞：＜1＞REFLECI SET；
REFLECT IF：＝IF LEUEL DF DETAII＞O THEN REFLECT；
〔
REFLECT，the vector list defining the reflection of all displayed structures about a plane，will be provided dynamically by the host computer．The command provided by the host will be of the form：
＊REFLECT：$=$ UECIOR＿LIST ITEMIZED $N=x \times x \times$＊ 3
〔
＊＊＊＊＊＊＊＊＊＊＊Display Intersection Uith XY Planes＊＊＊＊＊＊＊＊＊＊
3
XY SET：＝SET LEUEL OF DETAIL TD O THEN XY IF；
\｛Display intersection
if toggled on．\}
CDNNECT FETCHXYMODE＜1＞：＜1＞XY SET；
$X Y$ IF：＝IF LEUEL OF DETAIL＞O THEN XY；
\｛\}
XY：＝INSTANCE $\square F X Y C, X Y F ; \quad$ \｛The sturucture has two levels of display detail：coarse and Fines
XYF：＝IF LEUEL DF DETAIL＝己 THEN XYFINE；
〔
The structures XYC and XYFINE will be provided dynamically by the host computer．The commands provided will be of the form：

```
* XYC:=UECTDR LIST ITEMIZED N=xXX *
* XYFINE:= UECTDR LIST ITEMIZED N=xXX *
}
{
*********** Display Intersection With XZ Planes ***********
}
X2 SET:=SET LEUEL_DF _DETAIL ID O THEN XZ_IF;
                                    {Display intersection
                                    if toggled ח..}
            CDNNECT FETCHXZMDDE<1>:<1>XZ SEI;
XZ IF:=IF LEUEL DF DETAIL >O THEN XZ;
[}
```



```
X2:=INSIANCE OF X2C,X2F; {The sturucture has two
    levels of display
    detail: coarse and fines
    XZF:=IF LEUEL_OF_DETAIL =2 THEN XZFINE;
{
The structures XZC and XZFINE will be provided dynamically by the host computer. The commands provided will be of the form:
* \(\quad\) 2ZC: \(=\) UECTOR LIST ITEMIZED \(N=x \times x\)
* XZFINE: \(=\) UECTOR LIST ITEMIZED \(N=x \times x\)
3
YZ_SET: = SET LEUEL_ FF _DETAIL TD O THEN YZ_IF;
\{Display intersection
if toggled on. \(\}\)
CONNECT FETCHYZMODE<1>:<1>YZ SET;
YZ_IF:=IF LEUEL \(O F\) DETAIL >O THEN YZ;
\{\}
YZ: = INSTANCE \(O F Y Z C, Y Z F ; \quad\) \{The sturucture has two levels of display detail: coarse and fine\}
YZF: = IF LEUEL DF DETAIL =2 THEN YZFINE;
\{
The structures YZC and YZFINE will be provided dynamically by the host computer. The commands provided will be of the form:
* YZC: =UECTOR LIST ITEMIZED \(N=x \times x\)
* YZFINE: = UECTOR_LIST ITEMIZED \(N=x x x\)
3
\{
```



```
**************************************************************
*********************** Connect Dials ***********************
***************************************************************
**************************************************************
3
{
*************************************************************
********************* Translation Dials *********************
****************************************************************
```

 3
TRAN_X:=F:XUEC;
TRAN_Y: =F: YUEC;
TRAN Z: $=\mathrm{F}:$ ZUEC;
CONNECT DIALS<1>:<1>IRAN_X;
CONNECT DIALS<2>:<1>TRAN_Y;
CONNECT DIALSく3>:<1>TRAN_2;
ई
***** Create switching netwark which applies *****
***** translation dials to global translation (if in *****
***** modes 1 or 2 ), vertex translation (if in mode 3,*****
***** interactive mode), or no translation (mode $4, \quad$.****
***** I/O menu
3
SWITCH TRAN: $=$ F:CROUTE(4);
CONNECT TRAN_X<1>:<2>SWITCH_IRAN;
CONNECT IRAN_Y<1>:<2>SWITCH_TRAN;
CONNECT TRAN_Z<1>:〈ट>SWITCH_TRAN;
CONNECT FETCHMODE<1>:<1>SWITCH_TRAN;
\{
***** Connect switch to global translation node if in *****
***** made 1 or 2 . *****
3
TRAN_TOTAL: =F:ACCUMULATE; \{Accumulator for global
translation. 3
CONNECT SWITCH TRAN<1>:<1>TRAN_TOTAL;
CONNECT SWITCH TRAN<2>:<1>TRAN TOTAL;
\{SWITCH_TRAN<3> will be connected later\}
CONNECT SWITCH_TRAN<4>:<1>DISCARD;
CONNECT TRAN TOTAL<1>:<1>ALL.TRAN;
\{\}
SEND U(0,0,0) TO <2>TRAN TOTAL;
\{Reset value for
translation. 3
SEND 1 TO <4> IRAN TOTAL;
SEND FIX(1) TO <1>SWITCH_TRAN;
\{Signal multiplier for
dial sensitivity?
\{Default initially to
mode 13


〔 Switch will be connected to control point translation nodes at a later point in the program． 3

## 〔

3

XMUL：$=$ F：MULC；$\quad$\begin{tabular}{l}

| $M$ Mltipliers for dial |
| :--- |
| sensitivity |

\end{tabular}

YMUL：＝F：MULC；
ZMUL：＝F：MULC；
CONNECT DIALS＜5＞：＜1＞XMUL；
CONNECT DIALS＜B＞：＜1＞YMUL；
CONNECT DIALS＜7＞：＜1＞2MUL；
\｛\}
ROIX：$=\mathrm{F}:$ XROTAIE；$\quad$ CConvert dial signal to
ROTY：$=F:$ YROTATE；
ROTZ：＝F：ZROTATE；
CONNECI XMUL＜1＞：＜1＞ROIX；
CONNECI YMUL＜1＞：＜1＞ROTY；
CONNECT 2MUL＜1＞：＜1＞ROIZ；
\｛\}
ROI＿ACCUM：＝F：CMUL；\｛Accumulator for rotations\}
CONNECT ROT＿ACCUM＜1＞：＜1＞ALL．ROT； CONNECT ROT＿ACCUM＜1＞：＜1＞RDI＿ACCUM；
\｛\}
RESET X：＝F：XROTATE；\｛Upon signal from host computer，resets accumulator with given $X$ rotation and $O$ Eor $Y$ and 2.3

CONNECT RESET＿X＜1＞：＜1＞ROI＿ACCUM；
RESET＿Y：＝F：YROTATE；$\quad$＿Upon signal from host computer，adds $Y$ rotation reset value to accumulator and triggers accumulator to Fire．3
CONNECT RESET＿Y＜1＞：＜2＞ROI＿ACCUM；

## 〔

Create switching netwark for ROTATE Eunction which will raute dials to global rotation node in all modes（ $1-3$ ），except when in interactive ＊＊＊＊＊mode（4），in which case no transformations are ＊＊＊＊＊allowed．

```
SWITCH ROI:=F:CROUTE(4);
    CONNECT ROIX<1>:<2>SWIICH ROI;
    CONNECI ROIY<1>:<2>SWITCH_ROI;
    CONNECI ROIZ<1>:<2>SWIICH ROI;
    CONNECI SWITCH_ROT<1>:<2>ROI_ACCUM;
    CONNECT SWITCH_ROT<2>:<2>ROI_ACCUM;
    CONNECT SWITCH_ROT<3>:<2>ROT_ACCUM;
    CONNECT SWITCH ROI<4>:< < > DISCARD;
    CONNECI FETCHMODE<1>:<1>SWITCH_ROI;
{
********** Send initial values to ratation network.
}
SEND 2OO TO <2>XMUL; {Multiplication factor
SEND 2OO TO <2>YMUL;
SEND 2OO ID <2>2MUL;
SEND FIX(1) IO <1>SWITCH_ROT; {Default initially to
mode 1}
SEND M3D(1,0,0 0,1,0 0,0,1) TO < 1>ROI_ACCUM;
                                    {Prime accumulator}
{
}
SWIICH_SCALE:=F:CRDUTE(4);
```

\{See SWITCH ROT above for description\}

```
SCALE: \(=F:\) DSCALE;
CDNNECT DIALS<4>:<2>SWITCH SCALE;
CONNECT SWITCH SCALE<1>: <1>SCALE;
CDNNECT SWITCH SCALE<2>:<1>SCALE;
CONNECI SWITCH SCALE<3>:<1>SCALE;
CONNECT SWIICH_SCALE<4>:<1>DISCARD;
CONNECI SCALE<1>:<1>ALL.SCALE;
\{\}
SEND FIX(1) TO <1>SWITCH SCALE;
〔Default initially to made 1\(\}\)
SEND 1 TO <2>SCALE;
SEND 1 TO <3>SCALE;
SEND 20 TO < 4 SCALE;
SEND 0.1 TO < S>SCALE;
```


## [\}

```
CONNECT FETCHMODE<1>:<1>SWIICH SCALE;
```

3
\｛
＊＊＊＊＊Enable picking when stylus tipsuitch is pressed．＊＊＊＊ 3
PICK＿IF＿MODE $3:=F:$ CROUTE（4）；
CONNECT FETCHMODE＜1＞：＜1＞PICK＿IF MODE3；
CONNECT TABLETIN＜4＞：＜2＞PICK＿IF MODE3；
ESends＇IRUE＇when
tipsuitch pressed\}
CONNECT PICK＿IF＿MODE3＜1＞：＜1＞DISCARD；
\｛Only regard stylus if
in interactive mode（3）\}
CONNECT PICK＿IF＿MODE3＜2＞：＜1＞DISCARD；
CONNECT PICK＿IF MODE3＜4＞：＜1＞DISCARD；
\｛\}
PICKMODE＿IOGGLE1：＝F：CROUTE（2）；\｛Directs＇true＇to proper set．picking node， depending on whether in single point or row pick modes 3
CONNECI FETCHPICKMODE＜1＞：＜1＞PICKMODE＿IOGGLE1；
\｛See variables\}
CONNECI PICK＿IF＿MODE3＜3＞：〈2＞PICKMODE＿IOGGLE1；
〔Passes＇TRUE＇to SEI PICKINE node anly if in mode 33
CONNECT PICKMODE IOGGLE1＜1＞：＜1＞CP＿PI．SEIPICK； CONNECI PICKMODE＿IOGGLE1＜2＞：＜1＞CP＿IINES．SETPICK；
\｛
＊＊＊＊＊Convert cursar position to picklist identifying
＊＊＊＊＊＊＊＊
the campanent picked． 3

CONNECT TABLETIN＜5＞：＜1＞PICK；\｛Send cursar coardinates to＇PICK＇for conversian to picklist\}
CONNECT PICKくこ〉：＜2＞PICKMODE TOGGLE1；
［Send＇FALSE＇to
SEI＿PICKING node to disable picking ance pick occurs\}
CONNECI PICK＜3＞：〈2＞PICKMODE TOGELE1；
\｛Disable picking if timeaut occurs uithout a pick\}


Convert picklist info to integer identifying the vertex picked．
\}
PICK＿ID：$=$ F：PICKINFD；$\{$ Extracts pick ID（i．e． ＇CP32＇）from picklist\}
CDNNECT PICK＜1＞：＜1＞PICK＿ID；
\｛\}
PICKMODE＿TOGGLE2：$=\mathrm{F}:$ CROUTE（2）；

ESends pick index if picking a row of vertices，discards it if picking individual vertex．\}
CONNECT FETCHPICKMODE<1>:<1>PICKMODE TOGGLE己;
CONNECI PICK_ID<1>:〈こ>PICKMODE_TOGGLE己;
CONNECI PICKMODE_IOGGLE2<1>:<1>DISCARD;
\{\}
PICKMODE TOGGLE $3:=\mathrm{F}: \operatorname{CRDUTE}(2) ; \quad$ SSends pick ID if
picking individual
vertex, discards it if
picking a row of
vertices.\}
CONNECT FETCHPICKMODE<1>:<1>PICKMODE TOGGLE3;
CONNECT PICK_ID<2>:<2>PICKMODE TOGGLE3;
CONNECI PICKMODE TOGGLE3<2>:<1>DISCARD;
CONNECT PICK ID<3>: <1>DISCARD;
CDNNECT PICK ID<4>:<1>DISCARD;
CONNECI PICK ID<5>:<1>DISCARD;
CDNNECT PICK ID<6>: <1>DISCARD;
CONNECT PICK ID<7>: <1>DISCARD;
CONNECT PICK_ID<8>: <1>DISCARD;
\{\}
PICK ASCII: =F:CHARCDNUERT; \{Converts characters of
pick ID to stream of
integers representing
ASCII equivalents\}
CDNNECT PICKMODE TOGGLE3<1>:<1>PICK ASCII;
\{Provides pick ID for
conversion to ASCII\}
SEND TRUE TO <2>PICK ASCII;
[\}
DIGITS: $=\mathrm{F}:$ SUBC; $\quad$ COnverts ASCII codes of
pick ID characters to
numeric digits.\}


CONNECI PICK ASCII＜1＞：＜1＞DIGITS；
〔Provides ASCII－coded pick ID Ear conversion\} SEND FIX（48）IO＜2＞DIGITS；\｛Subtract 48 from ASCII code？
\｛\}
SWITCH＿DIGIT：＝F：ROUIE（4）；
\｛Ihis switch will send each of the four numerals from the converted pick ID for separate processing\}
CONNECI DIGITS＜1＞：＜2＞SWITCH＿DIGII；
\｛Provides the pick ID digits to the switch\}

## $\{$

The following is a toggling network which provides an input of integers which progress from 1 to 4 ，then start again， to the switch．Ihis causes each of the four successive digits from the converted pick ID to be routed to the corresponding output part far pracessing．

TRIGGER＿TOGGLE：$=F:$ CONSTANT；
\｛For each digit
received of the pick ID，
sends a 1 to ADD＿ONE\}
SEND FIX（1）TO＜2＞TRIGGER＿IOGGLE； CONNECT PICK＿ASCII＜1＞：＜1＞TRIGGER＿TOGGLE；

〔Provide a signal to
trigger the toggle\}
ADD＿ONE：$=\mathrm{F}:$ ADD；\｛Provides an integer
which increases by 1
each time a digit is
sent of the pick ID\}
CONNECT TRIGGER＿TOGGLE＜1＞：＜1＞ADD＿ONE；
〔Supply the 1 to be
added each time？
CONNECT ADD＿ONE＜1＞：＜2＞ADD＿ONE；
〔Supply the sum back to the input Far
incrementing next times
SEND FIX（3）TO＜2＞ADD ONE；
\｛Prime the summing
functions
\｛\}
CYCLEO＿3：$=\mathrm{F}:$ MODC；
\｛Converts the constantly increasing autput Eram ADD＿DNE to an integer cycling from 0 through 33
CONNECT ADD＿ONE＜1＞：＜1＞CYCLEO＿3；
SEND FIX（4）ID＜2＞CYCLEO＿3；


```
CYCLE1_4:=F:ADDC;
    {Converts 0-3 cyclic
    output from previous
    Function to 1-4 cyclic
    output}
    CONNECT CYCLEO_3<1>:<1>CYCLE1_4;
    SEND FIX(1) TO <2>CYCLE1_4;
```

\{\}
CONNECT CYCLE1_4<1>:<1>SWITCH_DIGIT;
〔Provide integers 1-4 to
control switch\}
CONNECT SWITCH_DIGIT<1>:<1>DISCARD;
[Discard the "CP"
prefix
CONNECT SWITCH_DIGIT<2>:<1>DISCARD;
TENS DIGIT: F:MULC;
CMultiplies tens digit
of ID number by 103
SEND FIX(1O) TO 〈2>TENS_DIGIT;
CONNECT SWITCH_DIGIT<3>:<1>TENS_DIGIT;
\{Provides first of two
digits of ID number for
conversion to tens.\}
[\}
PICKED_CP: =F:ADD;
〔Reconstructs the ID
number of the picked
vertex from the separate
ones and tens digits
CONNECT TENS DIGIT<1>:<1>PICKED CP;
CONNECT SWITCH_DIGIT<4>:<2>PICKED_CP;
\{\}
PICKED: =F:NOP;
〔Provides a node for
other other partions of
the program to obtain
the picking ID from, and
for the host computer to
send it to in some
cases. 3
CONNECT PICKED_CP<1>:<1>PICKED;
〔


# If picking rows and columns of vertices，pass the pick index to the host computer for conversion to a number identifying the row or column to be connected to the translation dials． 

\}
OFFSET＿PICK：＝F：ADDC；\｛Adds offset to pick index to put it into range which the host program recognizes as identifying a pick index． 3
CONNECT PICKMODE TOGGLE2＜2＞：＜1＞OFFSET＿PICK；
SEND FIX（100）TD＜2＞ロFFSET＿PICK；
CONNECT $\quad$ FFFSET＿PICK＜1＞：＜1＞TD＿HDST；
〔
After conversion by the host to a number identifying the row or column picked，the identifier is returned from the hast in the farm：
＊SEND FIXC ）ID＜1＞PICKED
3
〔
Establish a switch which directs the output of the translation dials，when in mode 3 ， to the translation node of the selected vertex．
3
SWITCH＿PICK：＝F：CROUTE（98）；
\｛A switch with 98 positions．The First 80 are for the 80 vertices， the next ten for the ten rows of vertices，and the last eight are for the columns of vertices 3
CONNECT SWITCH＿TRAN＜3＞：＜2＞SWITCH＿PICK；
〔Provide the dial output to the switch if in
interactive mode（3）．3
\｛In the program section which reports vertex movement to the host computer，the value in PICKED will be reported to＜1＞SWITCHPICK to provide the identifying number of the selected vertex to the switch．3

〔
The FORTRAN program on the host computer will provide PS－300 commands which will connect the outputs of the switch to the inputs of the translation accumulators of the vertices．These commands will be of the form：
＊CONNECT SWITCH＿PICK＜32＞：＜1＞TRAN＿TOTAL 32
3


## It

## 〔

＊＊＊＊＊＊＊＊＊Report Vertex Movement to Host Computer

3
CP MDUE ：$=F$ ：ACCUMULATE；
\｛Accumulates translation dial signals if in mode
3 （interactive mode）． 3
CONNECT SWITCH＿TRAN＜3＞：＜1＞CP＿MDUE； SEND U（O，O，0）TD＜2＞CP MDUE； SEND 0.001 TD＜ヨ＞CP＿MDUE；
\｛Report accumulation at this interval．\}
SEND 0.1 TD＜4＞CP MDUE；
\｛Scale signal to match scaling at individual vertex accumulators．3
RESET＿CP＿MOUE：$=F$ ：CONSTANT； ［Resets accumulator to 0 each time the
accumulator fires，so
only delta values are
sent to host computer． 3
CONNECT CP MOUE〈1＞：＜1＞RESEI＿CP MQUE； SEND U（O，O，O）TD＜2＞RESEI＿CP＿MDUE； CONNECT RESET＿CP MOUE＜1＞：＜2＞CP MOUE；

MOUE SYNC：$=$ F：SYNC（2）；\｛Ensures that currently picked vertex identifier is reported to the host computer immediately before the vertex position delta is reported． 3
MOUE＿THIS＿DNE：$=F:$ CONSTANT；
\｛Sends the current picked vertex identifier to MOUE SYNC each time the CP＿MOUE accumulator fires．${ }^{\text {f }}$
CDNNECT CP＿MDUE＜1＞：＜1＞MDUE＿IHIS＿ONE；
\｛PICKED2＜1＞will be connected to
＜2＞MDUE THIS DNE below．\}
CONNECT MOUE THIS ONE＜1＞：＜1＞MOUE SYNC；
CONNECT CP＿MOUE＜1＞：〈ट＞MOUE＿SYNC；
\｛\}
CONNECT MOUE＿SYNC＜1＞：＜1＞TO HOST；
CONNECT MOUE＿SYNC＜2＞：＜1＞TO＿HOST；
\｛


Before reusing the accumulator，CP MDUE，for
＊＊＊＊＊another vertex，report any remnant in the
＊＊＊＊＊accumulator to the host computer．
3
ZERD：$=\mathrm{F}:$ CONSIANT；

CONNECI PICKED＜1＞：＜1＞2ERD；

SEND O TO＜2＞ZERD；
UECZERD：＝F：CONSTANT；

CONNECT ZERD＜1＞：＜1＞UECZERD；

SEND U（O，O，0）ID＜ 2 ）UECZERD； ZERD＿FIRSI：－F：SYNC（2）；
\｛Pravides a zera to be sent to＜3＞CP＿MDUE， allowing accumulator to Fire without waiting to reach normal firing increment． 3
\｛Irigger the accumulator firing increment to be reset to zero whenever a new vertex is picked for movement． 3

SSends a zera vector to ＜1＞CP＿MDUE，causing the accumulator to Eire． 3
\｛Send the zero vector when triggered by output from ZERD．3

〔Ensures＜3＞CP MDUE is set to zero before ＜1＞CP MOUE is provided with signal to fire accumulator．\}
CONNECT ZERD＜1＞：＜1＞ZERD＿FIRST；
CONNECT UECZERD＜1＞：〈こ〉ZERD＿FIRST；
CONNECI ZERD＿FIRST＜1＞：〈3＞CP MDUE；
CONNECI ZERDFIRSI＜2＞：＜1＞CP MDUE；
STEP＿SIZE：＝F：CONSTANT；\｛AEter CP MOUE fires， resets CP MOUE Firing increment． 3
CONNECI CP MQUE＜1＞：＜1＞STEP SIZE；
SEND 0．005 ID＜ट＞STEP SIZE；
CONNECT STEP SIZE＜1＞：〈3＞CP MDUE；
SET＿PICKED2：＝F：CONSTANT；
〔Sends new value of PICKED to PICKED2，after any remnant in the CP＿MOUE accumulator has been dumped to the host for addition to the position of the previously picked vertex．\}
CONNECT PICKED＜1＞：＜2＞SET＿PICKED2；
CONNECT STEP＿SIZE＜1＞：＜1＞SEI＿PICKEDZ；

PICKED2：＝F：NDP；
\｛Contains identifier of currently selected vertex，but is not updated until CP＿MDUE accumulator remnant has been reported in accordance with previous value of PICKED2．3
CONNECT SET＿PICKED2＜1＞：＜1＞PICKED2；
CONNECI PICKED2＜1＞：＜1＞SWIICH PICK；
\｛See SWITCH＿PICK near end of Vertex Picking Network． 3
CONNECT PICKED2＜1＞：〈こ〉MOUE＿THIS＿ONE；
\｛See MOUE＿SYNC above．\}
SEND FIX（1）TQ＜1＞PICKEDE；

3
CLIP＿TRUE：＝F：INPUIS＿CHOOSE（3）；$\quad$ ；Send a FALSE if clip－ ping is off，IPUE if clipping is on．\}
SEND FALSE TD ＜1＞CIIP TPUE；
SEND TRUE ID＜ट＞CLIP＿IRUE；
CONNECT FETCHCLIPMODE＜1＞：＜3＞CLIP＿TPUE；
CONNECI CLIP＿IRUE＜1＞：＜1＞CLIPON；\｛Ēnable clipping．\}
CONNECT CLIP＿TRUE＜1＞：＜1＞CLIP＿INTENSITY；
\｛Disable depth cueing\}
CLIP＿DIAL：＝F：CROUTE（2）；
〔Routes signal from dial
8 to control clipping window width if clipping enabled． 3
CONNECT FEICHCLIPMODE＜1＞：＜1＞CLIP DIAL；
CONNECI DIALSく8＞：＜ट＞CLIP＿DIAL；
CDNNECT CLIP＿DIAL＜1＞：＜1＞DISCARD；
〔Discard signal from
dial 8 if clipping not enabled． 3
CLIP＿TOTAL：$=F:$ ACCUMULATE；
\｛Accumulate dial signal\} CONNECT CLIP＿DIAL＜2＞：＜1＞CLIP＿TOTAL；

〔Routes signal fram dial to accumulator only if clipping is on CCLIPMODE $=23$
SEND 0．5 TD＜2＞CLIP TOTAL；\｛Reset value．\}
SEND 0.1 TO＜4＞CLIP＿IOTAL；
〔Scale dial signal and convert to real number．3

```
    SEND 1 IO <5>CLIP_TOTAL; {Maximum clipping width}
    SEND 0.OO2 IO <E>CLIP_IOTAL; {Minimum clipping width}
CLIP_SYNC:=F:SYNC(2); {Ensures clipping window
    limit is reset before
    the new window matrix is
    sent to CLIPPER.}
    CONNECI CLIP_TOIAL<1>:<1>CLIP_SYNC;
    CONNECI CLIP_IQIAL<1>:《己>CIIP-SYNC;
WINDOW_MATRIX:=F:WINDOW;
    SEND -1 IO < ट>WINDOW_MATRIX;
    SEND 1 IO < 3>WINDOU_MATRIX;
    SEND -1 IO < 4>WINDOW MAIRIX;
    SEND 1 IO <5>WINDOU_MAIRIX;
    SEND O IO <E>WINDOW_MATRIX; {Front Z-clipping plane}
    CONNECI CLIP SYNC<1>:<7>狽NDOW_MATRIX;
    {Back Z-clipping plane
    defined by dial signal}
    CONNECI CLIP_SYNC<こ>:<1>WINDOW_MATRIX;
                                    {Trigger WINDOW_MATRIX
                                    to send new matrix.}
CDNNECI WINDOW_MAIRIX<<1>:<1>CLIPPER;
{
************** Make Function Keys Operational
}
KEY_DFFSET:=F:ADDC;
\｛Add offset to function key signals to put them into range which host computer program recognizes as indicating a pressed Function key\}
SEND FIX（300）TO＜2＞KEY＿OFFSET； CONNECI FKEYS＜1＞：＜1＞KEY＿DFFSEI； CONNECT KEY＿ロFFSEI＜1＞：＜1＞ID＿HOSI；
```


## \｛



3
KEY1: =F:INPUTS_CHODSE(5);
SEND 'UERTICES' TO < 1>KEY1;
SEND 'UERTICES' ID <2>KEY1;
SEND 'UERTICES' TD <3>KEY1;
SEND 'PRI UERT' ID < $4>$ KEY1;
CONNECT FETCHMODE<1>: <5>KEY1;

CONNECT KEY1<1>:<1>FLABEL1;
KEY2: =F:INPUIS_CHOOSE(5);
SEND 'B-SPLINE' ID <1>KEY己;
SEND 'B-SPLINE' IO <2>KEYZ;
SEND 'B-SPLINE' IO <3>KEYZ;
SEND , ' TO < $4>$ KEYZ;
CONNECT FETCHMODE<1>:<5>KEY2;
CONNECT KEY2<1>:<1>FLABEL2;
KEY3: =F:INPUTS_CHOOSE(5);
SEND 'KNOWN PI' ID < $1>$ KEY 3 ;
SEND 'KNOWN PI' IO <2>KEY3;
SEND 'KNOWN PI' ID <3>KEY3;
SEND ', TD < 4 人KEY 3 ;
CONNECT FETCHMODE<1>:<5>KEY3;
CONNECT KEY3<1>:<1>FLABEL3;
KEY4: $=\mathrm{F}$ : INPUTS_CHOOSE (5);
SEND 'INTERACI' ID <1>KEYч;
SEND , ' TO < 2>KEY4;
SEND 'INIERACI' IO <3>KEY4;
SEND 'PLT SCRN' TD < $4>$ KEY ;
CONNECT FETCHMODE<1>:<5>KEY4;
CONNECI KEY4<1>:<1>FLABEL4;
\{\}
KEYS: =F:INPUTS CHOOSE(5);
SEND 'CLIP' TO < 1>KEYS;
SEND 'CLIP' TO <2>KEYS;
SEND 'CLIP' ID <3>KEYS;
SEND , TD < $4>$ KEYS;
CONNECT FETCHMODE<1>:<5>KEY5;
CONNECT KEY5<1>:<1>FLABELS;
\{\}
KEY5: $=\mathrm{F}$ : INPUTS CHOOSE(5);
SEND 'REFLECI' TO < $1>$ KEYE;
SEND 'REFLECI' TO <2>KEY5;
SEND , ' TD < 3>KEY5;
SEND ', TD < $\langle$ रKEYE;
CONNECT FETCHMODE<1>:<5>KEYE;
CONNECT KEYE<1>:<1>FLABELE;
\{Stores labels for FKEY 13
\{Natifies KEY1 of which label to use, depending on made.\}
\{Sends label to keyboard. $\}$


```
{}
KEY7:=F:INPUTS_CHOOSE(5);
    SEND 'XY' TO <1>KEY7;
    SEND 'XY' TO <2>KEY7;
    KEY7_MODE3:=F:INPUTS CHOOSE(3);
        SEND 'PICK RDW' TO <1>KEY7 MODE3;
        SEND , , TO <2>KEY7 MODE3;
        CONNECT FETCHPICKMODE<1>:<3>KEY7 MODE3;
        KEY7_SYNC:=F:SYNC(2);{Ensures new PICKMODE
                                    value is in place on
                                    KEY7 MODE3 before new
                                    MODE value is sent to
                                    KEY7, triggering that
                                    function.3
                                    CONNECT KEY7_MODE3<1>:<1>KEY7_SYNC;
                                    CONNECT FETCHMODE<1>:<2>KEY7 SYNC;
    CONNECT KEY7_SYNC<1>:<3>KEY7;
    SEND , TD <4>KEY7;
    CONNECT KEY7_SYNC<2>:<5>KEY7;
    CONNECT KEY7<1>:<1>FLABEL7;
{}
KEY日:=F:INPUTS_CHOOSE(5);
    SEND 'XZ' TO <1>KEY日;
    SEND 'XZ' TO <2>KEYG;
    KEY日_MODE3:=F:INPUTS_CHOOSE(3);
        SEND , TO <1>KEY日 MODE3;
        SEND 'PICK PT' TO <2>KEYQ MODE3;
        CONNECT FETCHPICKMODE<1>:<3>KEYB_MODE3;
                KEY日_SYNC:=F:SYNC(2);
                    CONNECT KEYB MODE3<1>:<1>KEYB SYNC;
                        CONNECT FETCHMODE<1>:<2>KEY日_SYNC;
    CONNECT KEYB_SYNC<1>:<3>KEYG;
    SEND 'SAU UERT' TO <4>KEYG;
    CONNECT KEYB_SYNC<2>:<5>KEYB;
    CONNECT KEYB<1>:<1>FLABELB;
{}
KEY9:=F:INPUTS_CHOOSE(5);
    SEND 'YZ' TO <1>KEYG;
    SEND 'YZ' TD <2>KEYG;
    SEND ' , TD <3>KEYG;
    SEND 'LD UERT' TO <4>KEYG;
    CONNECT FETCHMODE<1>:<5>KEYG;
    CONNECT KEY9<1>:<1>FLABEL9;
{}
KEY10:=F:INPUTS CHOOSE(5);
    SEND 'I/I' TO <1>KEY1O;
    SEND 'I/D' TO <2>KEY1O;
    SEND 'I/I' TD <3>KEY1O;
    SEND , , TO <4>KEY1O;
    CONNECI FETCHMODE<1>:<5>KEY1O;
    CONNECT KEY1O<1>:<1>FLABEL1O;
```



```
KEY11:=F:INPUTS_CHOOSE(5);
    SEND 'RESET' TD < 1>KEY11;
    SEND 'RESET' TD <2>KEY11;
    SEND 'RESET' ID <3>KEY11;
    SEND , , TD <4>KEY11;
    CDNNECT FETCHMODE<1>:<5>KEY11;
    CONNECT KEY11<1>:<1>FLABEL11;
{}
KEY12:=F:INPUTS_CHOOSE(5);
    SEND 'QUII' ID <1>KEY1己;
    SEND 'QUIT' ID < ट>KEY1己;
    SEND 'QUIT' TD <3>KEY12;
    SEND 'EXII I/ロ' TO<4>KEY12;
    CDNNECT FEICHMODE<1>:<5>KEY12;
    CDNNECT KEY12<1>:<1>FLABEL12;
{}
DIAL1:=F:INPUTS_CHOOSE(5);
    SEND 'GLOBAL X' TD < 1>DIAL1;
    SEND 'GLDBAL X' TO <ट>DIAL1;
    SEND 'UERTEX X' TD <3>DIAL1;
    SEND , , ID < 4>DIAL1;
    CDNNECT FETCHMODE<1>:<5>DIAL1;
    CONNECT DIAL1<1>:<1>DLABEL1;
{}
DIALC:=F:INPUIS CHOOSE (5);
    SEND 'GLOBAL Y' ID < 1>DIAL己;
    SEND 'GLDBAL Y' TO < <>DIAL己;
    SEND 'UERTEX Y' TD <3>DIAL己;
    SEND , ' TD <乡>DIAL己;
    CONNECT FETCHMODE<1>:<5>DIAL己;
    CDNNECI DIALट<1>:<1>DLABEL2;
{}
DIAL3:=F:INPUTS CHODSE(5);
    SEND 'GLOBAL Z' ID <1>DIAL3;
    SEND 'GLOBAL 2' TD < ב>DIAL3;
    SEND 'UERIEX Z' ID <3>DIAL3;
    SEND , , TD < 4>DIAL3;
    CDNNECT FETCHMODE<1>:<5>DIAL3;
    CONNECT DIAL3<1>:<1>DLABEL3;
{}
    BLINKER:=F:INPUTS CHOOSE(5); {Cause translation dials
                                    to blink when in inter-
                                    active mode.}
            SEND FALSE ID
            SEND FALSE ID
                SEND IRUE TD
    < 2>BLINKER;
SEND FALSE TD < <>BLINKER;
<3>BL INKER;
CONNECT FETCHMODE<1>:<5>BLINKER;
CONNECI BLINKER<1>:<2>DLABEL1;
CONNECT BLINKER<1>:<2>DLABEL己;
CONNECT BLINKER<1>:<2>DLABEL3;
```



```
{}
DIAL4:=F:INPUTS_CHODSE (5);
    SEND 'SCALING' ID < < >DIAL4;
    SEND 'SCALING' ID <<>DIAL4;
    SEND 'SCALING' ID <3>DIAL4;
    SEND, , TO < 4>DIAL4;
    CONNECT FETCHMODE<1>:<5>DIAL4;
    CDNNECI DIAL4<1>:<1>DLABEL4;
{}
DIAL5:=F:INPUTS_CHODSE(5);
    SEND 'ROTATE X' ID < 1>DIAL5;
    SEND 'RDIATE X' ID <2>DIALS;
    SEND 'RDIATE X' ID <3>DIAL5;
    SEND , ' TO < 4>DIALS;
    CONNECT FETCHMODE<1>:<5>DIAL5;
    CDNNECT DIAL5<1>:<1>DLABEL5;
{}
DIAL5:=F:INPUTS CHODSE (5);
    SEND 'RDIATE Y' ID <1>DIALE;
    SEND 'RDTATE Y' TO < ב>DIALG;
    SEND 'RDIATE Y' ID <3>DIALE;
    SEND , ' TO < 4>DIAL6;
    CONNECT FETCHMODE<1>:<5>DIAL5;
    CDNNECT DIALE<1>:<1>DLABELG;
{}
DIAL7:=F:INPUTS_CHODSE(5);
    SEND 'ROTATE Z' TO <1>DIAL7;
    SEND 'ROIATE 2' ID <2>DIAL7;
    SEND 'ROIATE Z' TD <3>DIAL7;
    SEND, , TO < 4>DIAL7;
    CONNECT FETCHMODE<1>:<5>DIAL7;
    CONNECI DIAL7<1>:<1>DLABEL7;
{}
DIAL8:=F:INPUTS CHODSE (3);
    SEND, , TO <1>DIALB;
    SEND 'CLIPPING' TD < ב>DIALB;
    CONNECT FEICHCLIPMODE<1>:<3>DIALQ;
    CONNECI DIALB<1>:<1>DLABELB;
{}
SEND 1 TD < 1>NEW MODE;
```

\{Irigger initial sending of default operating mode indicators. Whenever an operating mode indicator
(variable) changes, the host computer will send a similar triggering message. $\}$


# APPENDIX D <br> LINK COMMAND FILE 

The following is the command file used to link SPLINE.FIN with the various host-resident PS 300 library subroutines.

```
SPLINE/FP/CP/ID,=spline,bd
[1,1]MELIB/LB
[5,2OO]ENSNEW/LB
/
LIBR=F4PRES:RD
ACTFIL=4
UNITS=8
ASG=TT46:7
ASG=SYO:6
PRI=50
//
```

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©C. 1 A high-level computer graphics implementation of three-dimensional Bspline surface generation.

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